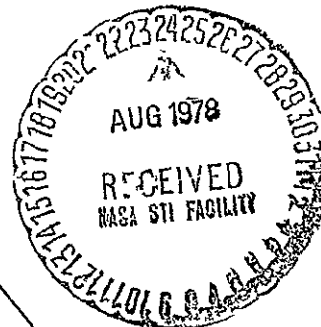


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EXTRAVEHICULAR ACTIVITY
TRANSLATION ARM (EVATA) STUDY

FINAL REPORT

ARC-TN-1064

by

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SECTION 1

INTRODUCTION

This report documents the preliminary design of a deployable Extravehicular Activity Translation Arm (EVATA) assembly which will allow an EVA crewman to perform tasks in the vicinity of the External Tank (ET) umbilical doors and to inspect most of the underside of the Shuttle spacecraft.

As conceived, the EVATA would stow in the last 48 inches of the Shuttle bay. The stowed package dimensions for this analysis were 40 inches wide, 58 inches deep, and 43 inches long. The deployed lengths as shown on NASA Drawing PD78-33600 were 46 feet for the upper boom and 63 feet of the lower boom.

The concept chosen for the boom structure was the Astro Extendable Support Structure (ESS) which formed the main structure for the Synthetic Aperture Radar (SAR) Antenna System on the SEASAT A spacecraft. The antenna system was successfully deployed in late June and the SAR was successfully operated in early July. This structure is a deployable triangular truss as shown in Figure 1.1. A comparison of the EVATA and the SEASAT A ESS is shown in Table 1-1. The development status of the ESS is shown in Table 1-2. The satellite configuration, the stowed truss load path, and the envelope deployment sequence for the ESS are shown in Figure 1-2. Figures 1-3, 1-4, and 1-5 show the actual SAR stowed, partially deployed, and deployed, respectively.

TABLE 1-1. COMPARISON OF EVATA AND SEASAT ESS STRUCTURE

	EVATA	ESS
OVERALL LENGTH	63 AND 46 FEET	35 FEET
PANEL LENGTH	34.5 INCHES	52.9 INCHES
PANEL WIDTH	39.1 INCHES	40 INCHES
TRUSS HEIGHT	19 INCHES	17.9 INCHES
TUBE MATERIAL	GRAPHITE/EPOXY	GRAPHITE/EPOXY
FITTING MATERIAL	6061-T6 ALUMINUM	6AL4V TITANIUM
TUBE DIAMETER	1.125 INCHES	0.5 INCH
TRUSS WEIGHT	TOTAL 2 BOOMS GR = 389 POUNDS AL = 767 POUNDS	30 POUNDS
PACKAGE SIZE	40 x 43 x 58 (10 INCHES FOR ELBOW)	55.5 x 55 x 8

TABLE 1-2. DEVELOPMENT STATUS OF EXTENDABLE SUPPORT STRUCTURE

One-half scale model demonstrated	December 1975
Full-scale model demonstrated	September 1976
SEASAT A SAR ESS tested and delivered	July 1977
SEASAT A launch	26 June 1978

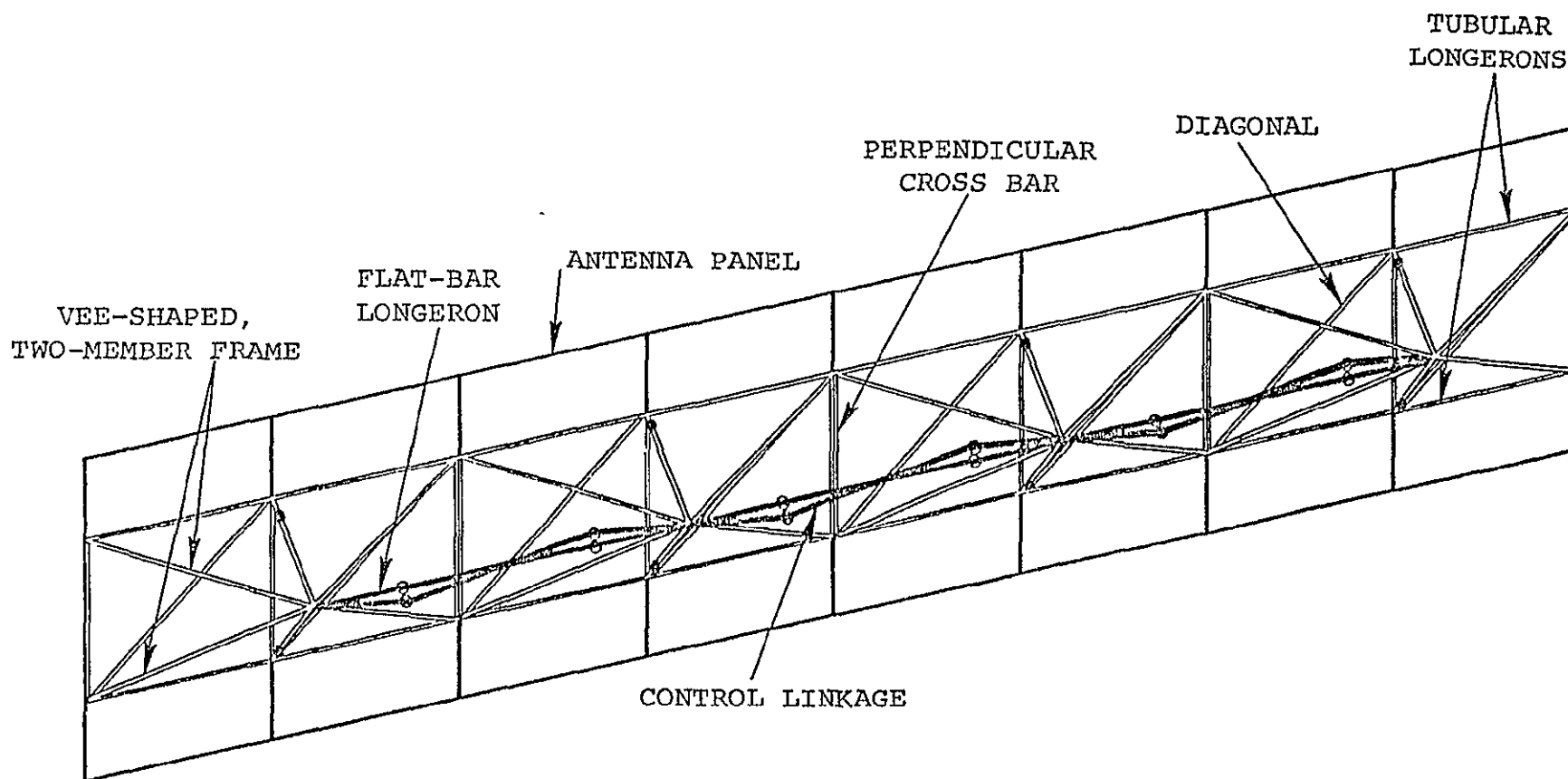
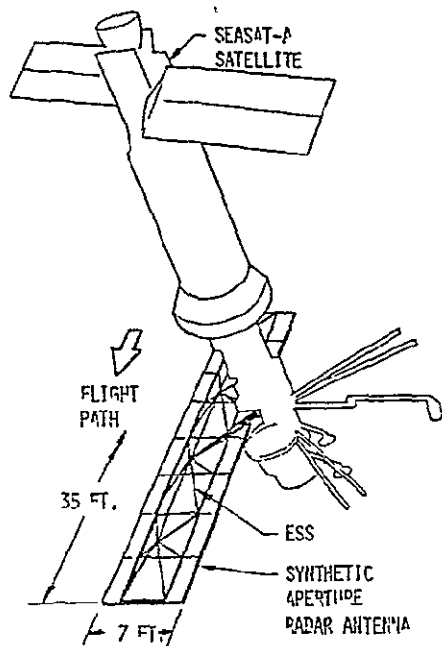
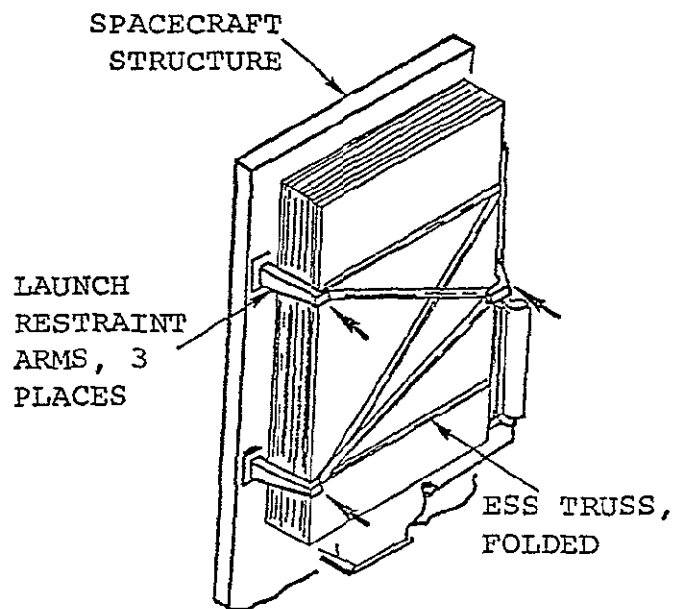


Figure 1-1. Deployed ESS.



Satellite Configuration.



Stowed Truss Load Paths.

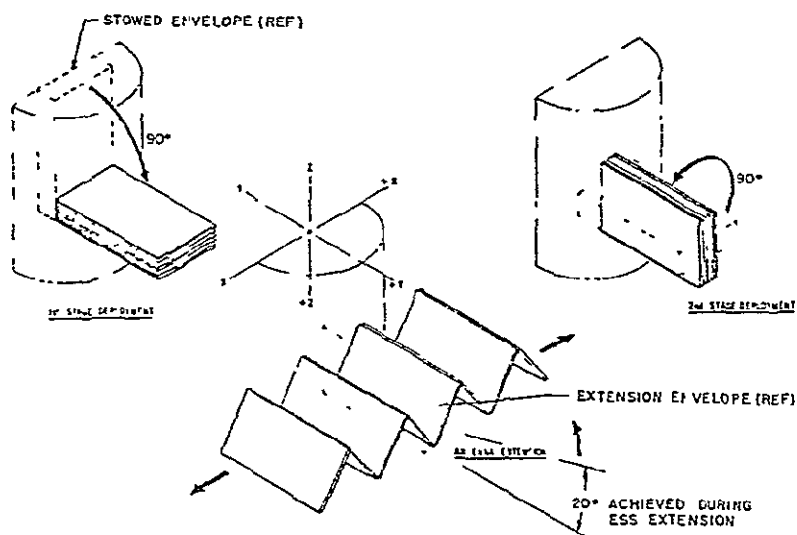


Figure 1-2. Envelope deployment sequence.

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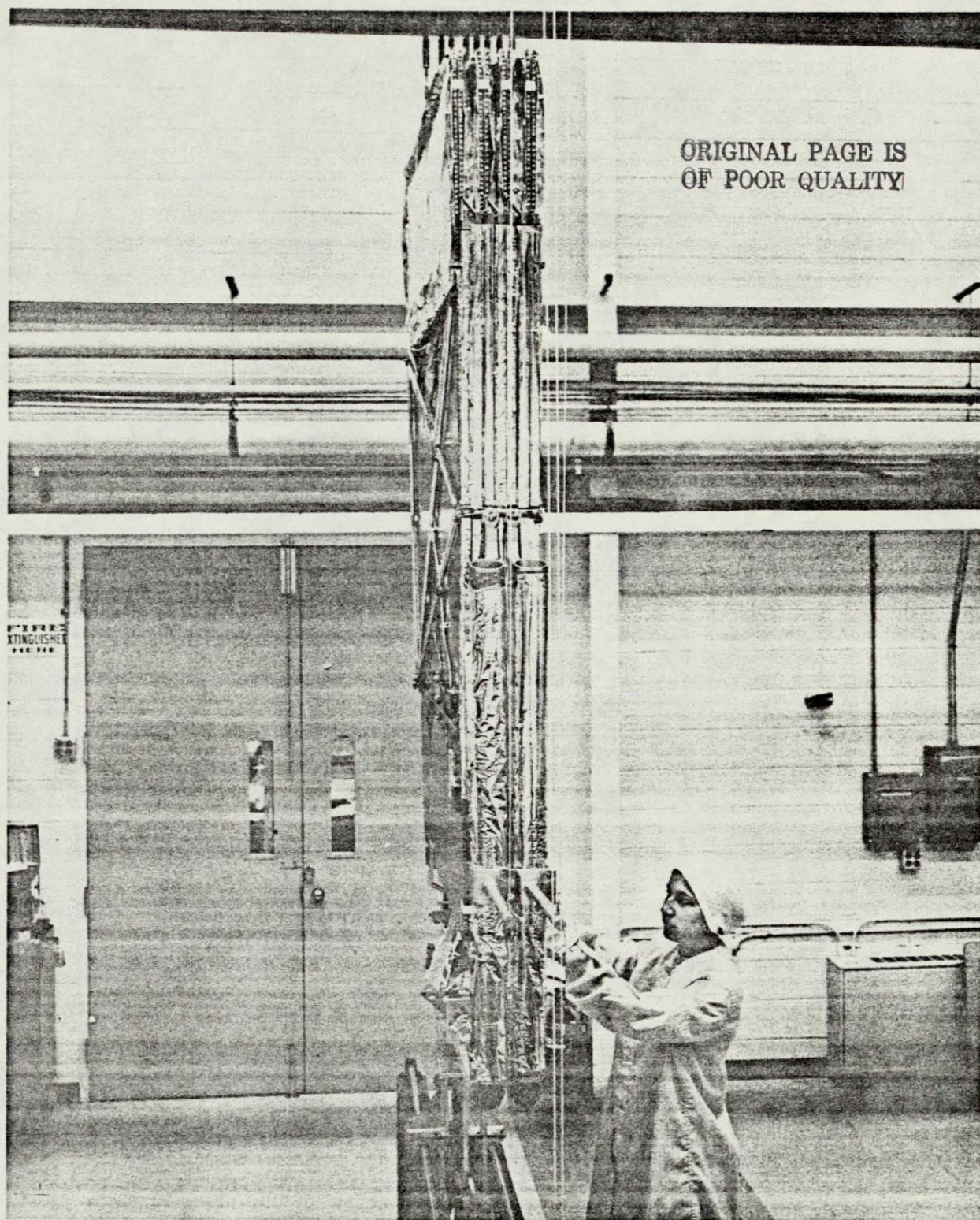
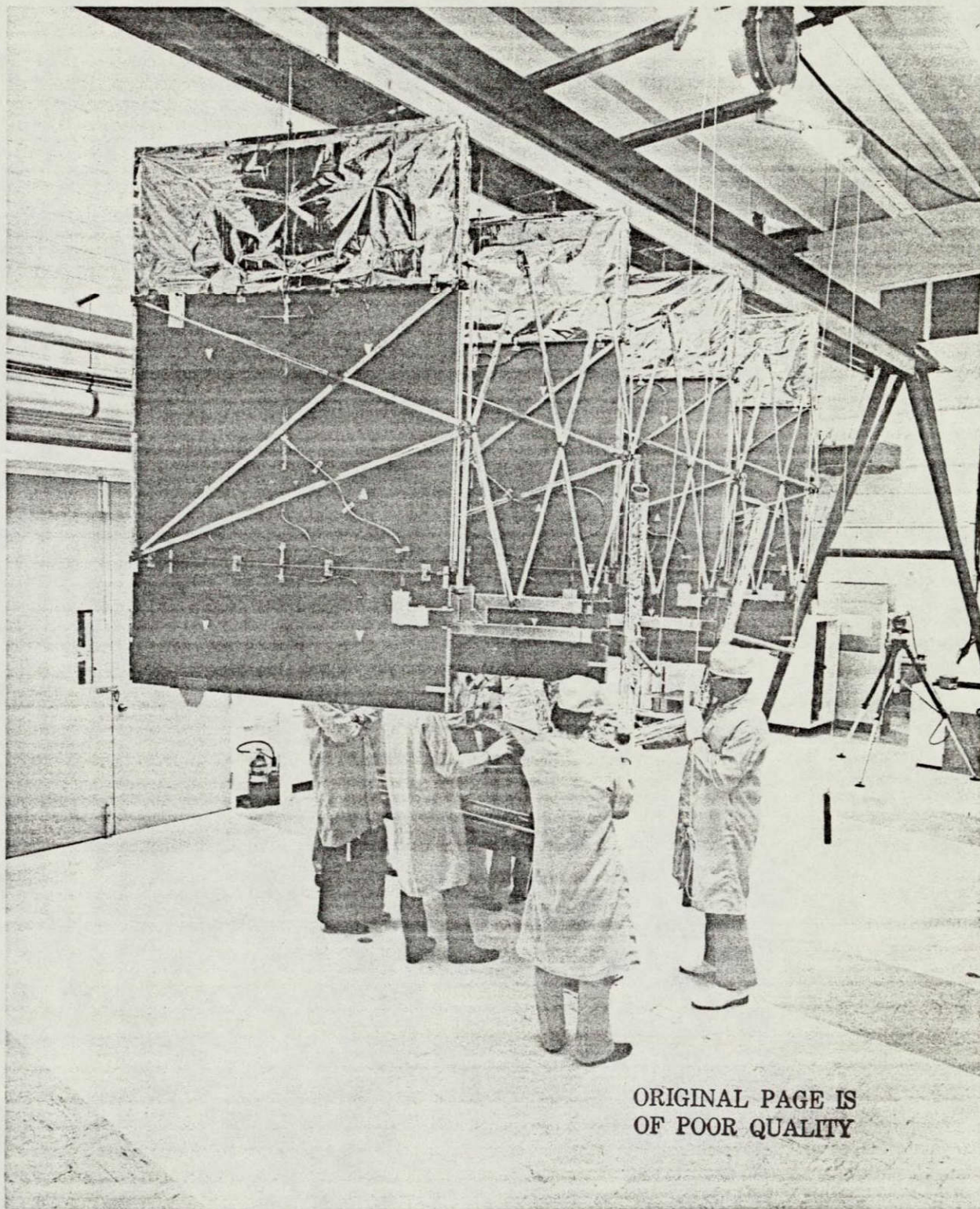


Figure 1-3. SAR stowed.



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Figure 1-4. SAR partially deployed.

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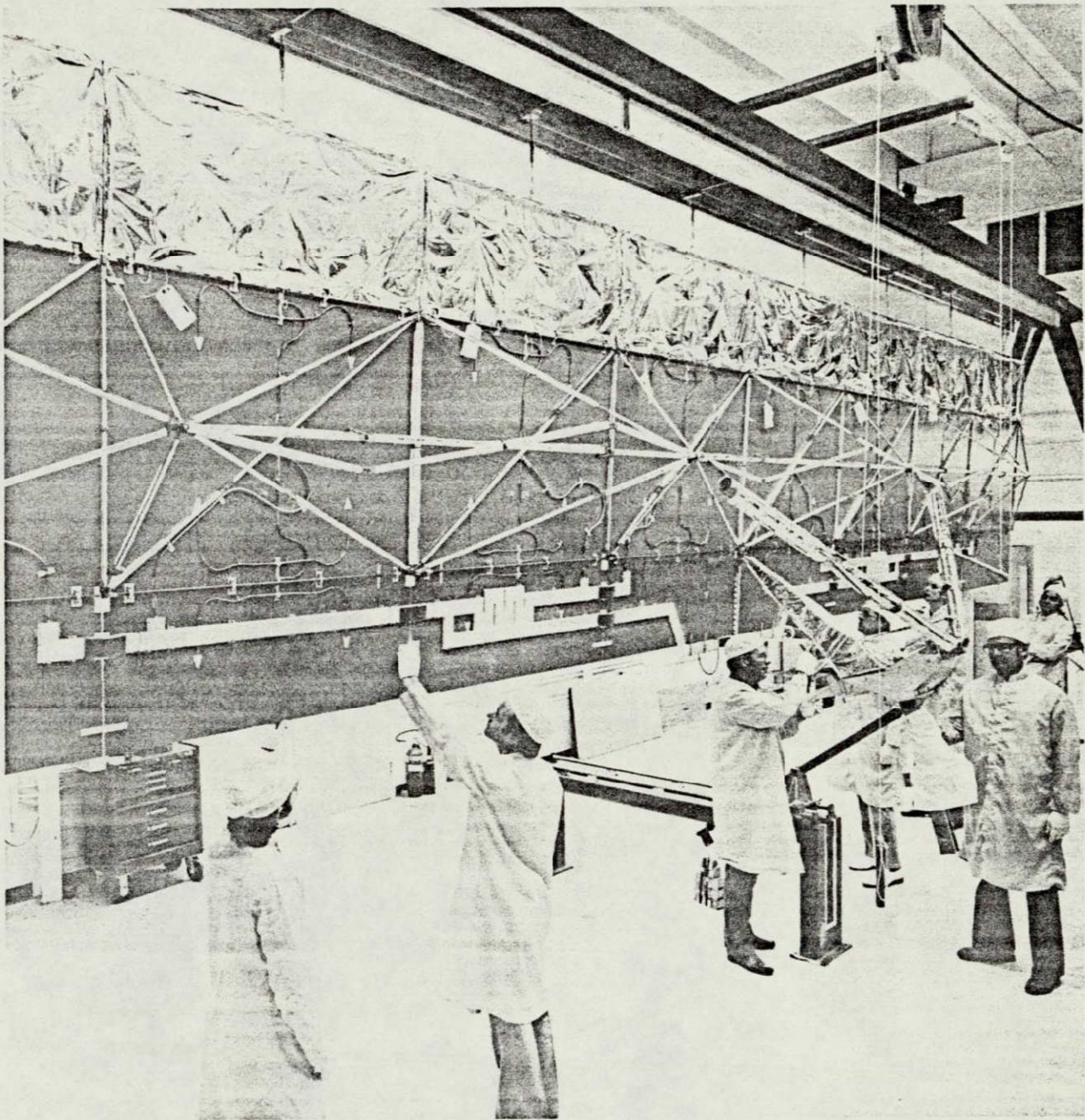


Figure 1-5. SAR deployed.

SECTION 2

GEOMETRY AND KINEMATICS OF THE TRUSS

2.1 CONSTRAINTS AND ASSUMPTIONS

The configuration of the truss is determined by the following constraints and assumptions:

- Package limitations and the length requirement for the extended truss confine the panel length to certain ranges, related to the number of panels, and limit the cross section of the longitudinal members. The lowest number of panels possible allows the largest truss depth and the biggest width of the longitudinal members; therefore, the stiffest configuration.
- The package space is best utilized when the width of the main scissor member equals the height of the longitudinal panel members. For practical reasons, all members are assumed to be cylindrical tubing of circular cross section. For additional simplification, all members except the control linkage of the scissor are of the same outer diameter.
- Again, for best package utilization, the knee braces fold into a position where both legs lie flat against each other and parallel to the cross braces. The gap shown in Figure 2-1 between upper knee brace and main scissor member is reduced to zero for the same reason.
- A highly efficient truss avoids load eccentricities at the joints, i.e., all axes of truss members pass through a common point in each joint. For simplification, this rule was broken only where the A-frame joins the front panels of the truss. There the same distance between truss-member axis and hinge axis was used for the panel members as well as the A-frame member. The resulting eccentricity is less than 10 percent of the member diameter.

2.2 SYSTEM OF CONDITIONS AND EQUATIONS

With the above restraints and the geometric relations depicted in Figures 2-1 and 2-2, the following system of conditions and equations are formulated.

$$N_u \ell \approx 550 \text{ in.}$$

length of upper arm

$$N_\ell \ell \approx 710 \text{ in.}$$

length of lower arm

$$(N_u + N_\ell) d_\ell \leq 58-10 \text{ in.}$$

length of package allowing room for elbow joint

$$\ell + 2g \leq w_p$$

width of package

$$d_\ell = d_{s1} = d_a = d_b = d_d = d_k$$

tubular members of same o.d.

$$d_p + h_a + c + \frac{d_{s1}}{2} + d_{s2} = h_p$$

package height

$$d_p + \ell + \frac{d_\ell}{2} + (k_3 + k_4) \cos \gamma + d_k + \frac{d_{s1}}{2} + d_{s2} = h_p$$

package height

$$b + 2(k_1 - k_3 \sin \gamma) + 2 d_{pk} = w_p$$

package width

$$2(k_2 + k_4 \sin \gamma) + 2 d_{pk} = w_p$$

package width

$$k_4 \cos \gamma - \frac{d_k}{2} - \frac{d_{s1}}{2} = 0$$

tight package

$$e + f - \frac{d_a}{2} = 0$$

tight package

$$c \tan \alpha - f \frac{1}{\cos \alpha} - e = 0$$

$$2(k_1 + k_2 + k_3 + k_4) \sin \gamma - b = 0$$

$$\frac{d_a}{2} \cos \alpha + h_a \sin \alpha + f \cos \alpha + e - \ell = 0$$

$$\frac{d_\ell}{2} - \frac{d_k}{2} \sin \alpha + h_a \cos \alpha - f \sin \alpha + c - (k_1 + k_2 + k_3 + k_4) \cos \gamma = 0$$

The first four equations allow the choice of N_u , N_ℓ , ℓ , and d_ℓ when the package width is given and the space needed for the special scissor hinges, g , is estimated.

The remaining 15 equations contain 23 variables of which two already have been determined, two (h_p and w_p) are either given or used as parameters, leaving another four as parameters. In this study, the hinge pin diameters, d_p and d_{pk} , were fixed as 0.1875 and 0.125, respectively, the thickness or diameter of the scissor control linkage was assumed as 0.5 inch, and the hinge location, e , was used as the variable parameter.

The following values were used for the configuration with the ladder (truss-face panel) in vertical and horizontal position, respectively.

<u>Variable</u>	<u>Vertical Ladder</u>	<u>Horizontal Ladder</u>
N_u	16	15
N_ℓ	22	20
ℓ	34.500	37.500
d_ℓ	1.125	1.250
w_p	43.00	40.00
h_p	40.00	Parameter
d_p	0.1875	0.1875
d_{pk}	0.125	0.125
d_{s2}	0.500	0.500

Three additional dimensions of the deployed truss are calculated once the above mentioned variables are all determined:

$$\text{truss height, } h = \sqrt{(k_1 + k_2 + k_3 + k_4)^2 - \frac{\ell^2}{4}}$$

$$\begin{array}{l} \text{theoretical length of} \\ \text{A-frame member, a} \end{array} = \sqrt{(k_1 + k_2 + k_3 + k_4)^2 + l^2}$$

$$\begin{array}{l} \text{theoretical length} \\ \text{of panel diagonal, D} \end{array} = \sqrt{b^2 + l^2}$$

2.3 BASELINE TRUSS DESIGN

The values for the baseline truss design, thus derived, are presented in Table 2-1.

TABLE 2-1. BASELINE TRUSS CONFIGURATION

Parameter	Vertical Ladder	Horizontal Ladder
Truss width, b	39.088	34.867
Truss height, h	18.933	30.194
Panel length, ℓ	34.500	37.500
Diagonal length, D	52.136	51.205
A-frame member, a	43.940	51.204
Knee brace length, \sum_k	27.211	34.866
A-frame angle, α	61.141°	50.994°
Knee brace angle, γ	45.910°	30.001°
Package width, w_p	43.00	40.00
Package height, h_p	40.00	48.766
Package depth		
Upper arm $N_u \times d$	18.00	18.75
Lower arm $N_\ell \times d$	24.75	25.00

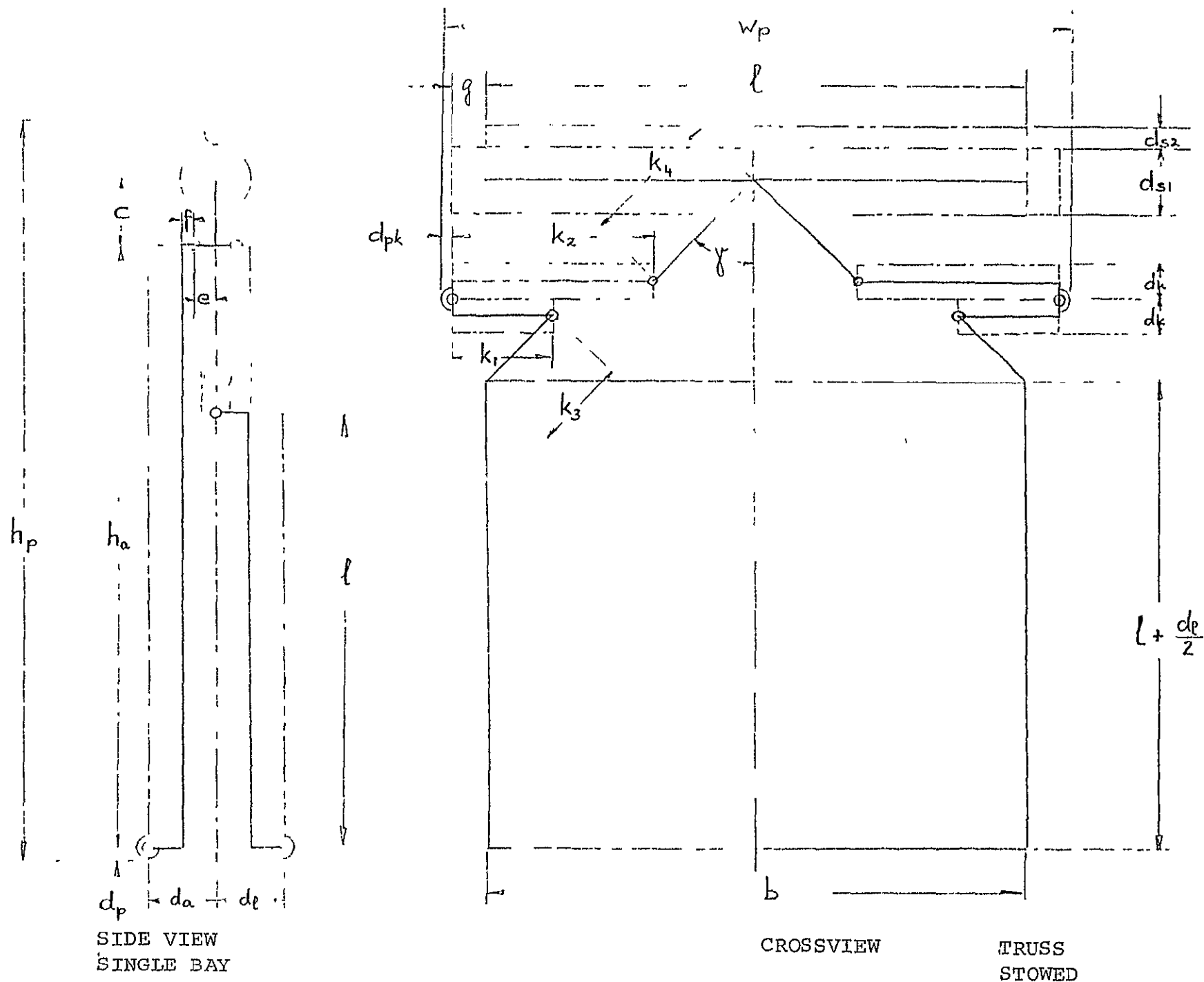
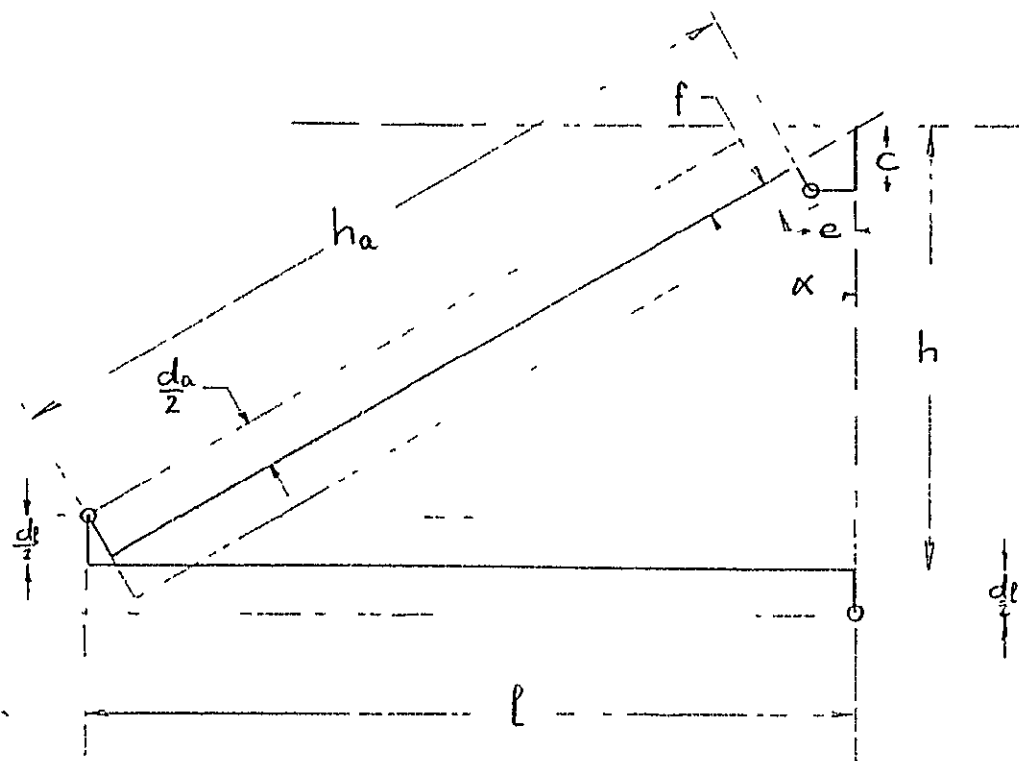
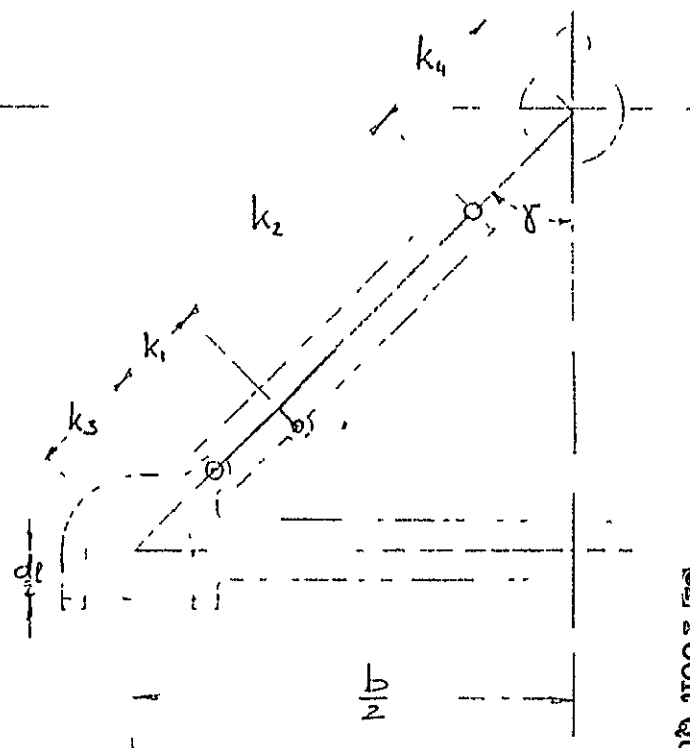


Figure 2-1. Schematic Geometry of Stowed Truss



SIDE VIEW
HALF BAY



CROSS VIEW
HALF BAY

Figure 2-2. Schematic geometry of deployed truss.

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SECTION 3

STRUCTURAL CHARACTERISTICS OF TRUSS

3.1 NOTATION AND CONVENTION OF FORCES

In order to determine strength and compliance of the truss with respect to external loads, a convention for the representation of external forces is established as shown in the lower right corner of Figure 3-1. The same figure shows the relations among internal forces as found from equilibrium considerations for each joint. A cut at distance x from the local coordinate origin provides the relations between external and internal forces:

$$\begin{aligned}
 P &= P_1 - \frac{l}{d} P_d + P_2 + P_3 + \frac{l}{a} (P_A + P_B) + \frac{l}{d} P_d - \frac{l}{a} (P_A + P_B) \\
 V_2 &= -\frac{b}{d} P_d + \frac{b}{2a} (P_A - P_B) \\
 V_1 &= \frac{h}{a} (P_A + P_B) \\
 Q &= \frac{h}{a} (P_A - P_B) \frac{b}{2} \\
 M_{10} - V_1 x &= -\left(P_3 + \frac{l}{a} (P_A + P_B)\right) h + \frac{l}{a} (P_A + P_B) h \left(1 - \frac{x}{l}\right) \\
 M_{20} - V_2 x &= \left(P_1 - \frac{l}{d} P_d - P_2\right) \frac{b}{2} - \frac{l}{d} P_d \frac{b}{2} \left(1 - \frac{2x}{l}\right) - \frac{l}{a} (P_A - P_B) \frac{b}{2} \frac{x}{l}
 \end{aligned}$$

Inversion of this equation matrix leads to the following system of equations for the internal forces. For details, see Appendix A.

$$\begin{aligned}
P_1 &= \frac{P}{2} - \frac{l}{b} V_2 + \frac{l}{bh} Q + \frac{M_{10}}{2h} + \frac{M_{20}}{b} \\
P_2 &= \frac{P}{2} + \frac{l}{b} V_2 - \frac{l}{bh} Q + \frac{M_{10}}{2h} - \frac{M_{20}}{b} \\
P_3 &= - \frac{M_{10}}{h} \\
P_A &= \frac{a}{2h} V_1 + \frac{a}{bh} Q \\
P_B &= \frac{a}{2h} V_1 - \frac{a}{bh} Q \\
P_d &= - \frac{d}{b} V_2 + \frac{d}{bh} Q
\end{aligned}$$

3.2 DETERMINATION OF FORCES

With these equations and Figure 3-1, the force in any of the truss members can be determined simply by reducing the external forces to the load vector in the symmetry plane of the module in question.

For a given external load condition, the strength of the truss is determined by comparing the loads of each truss member with its load capacity which may be limited either by yielding or buckling. It is assumed that the shear strength of the joint pins and the bearing strength of the joints are considerably higher than the strength of the truss members; but, in any case, this must be proven.

In order to establish the stiffness and compliance characteristics of the structure, the truss is considered equivalent to a beam of constant cross-sectional properties, namely bending stiffness about the two neutral axes, EI_1 and EI_2 ; center of gyration, e_1 and e_2 ; shear stiffnesses, GA_{S1} and GA_{S2} ; shear center, e_3 and e_4 ;

and torsional stiffness, GJ. These features are determined by comparing the strain energy of one truss module with that of an equally long (2 ℓ) beam section. When expressed as functions of the external loads, the truss properties can be found by comparing corresponding terms. Thus, as developed in Appendix B,

$$\frac{1}{EI_1} = \frac{1}{h^2} \left(\frac{1}{2(EA)_\ell} + \frac{1}{(EA)_s} \right)$$

$$\frac{1}{EI_2} = \frac{2}{h^2} \frac{1}{(EA)_\ell}$$

$$e_1 = \frac{h}{\left(1 + 2 \frac{(EA)_\ell}{(EA)_s} \right)}$$

$$e_2 = 0$$

$$\frac{1}{GA_{S1}} = \frac{\ell^2}{h^2} \frac{1}{6(EA)_\ell} \left[4 \frac{(EA)_\ell}{(EA)_s} + 3 \frac{a^3}{\ell^3} \frac{(EA)_\ell}{(EA)_a} - 1 \right]$$

$$\frac{1}{GA_{S2}} = \frac{2}{3} \frac{\ell^2}{h^2} \frac{1}{(EA)_\ell} \frac{\left[\left(\frac{a^3}{\ell^3} \frac{(EA)_\ell}{(EA)_a} - 1 \right) + \left(3 \frac{a^3}{\ell^3} \frac{(EA)_\ell}{(EA)_a} - 1 \right) \left(\frac{d^3}{\ell^3} \frac{(EA)_\ell}{(EA)_d} + \frac{1}{2} \frac{\ell^3}{\ell^3} \left(\frac{(EA)_\ell}{(EA)_{b_1}} + \frac{(EA)_\ell}{(EA)_{b_2}} \right) \right) \right]}{\left[1 + 2 \frac{a^3}{\ell^3} \frac{(EA)_\ell}{(EA)_a} + \frac{d^3}{\ell^3} \frac{(EA)_\ell}{(EA)_d} + \frac{1}{2} \frac{\ell^3}{\ell^3} \left(\frac{(EA)_\ell}{(EA)_{b_1}} + \frac{(EA)_\ell}{(EA)_{b_2}} \right) \right]}$$

$$e_3 = h \frac{\left[1 + \frac{d^3}{\ell^3} \frac{(EA)_\ell}{(EA)_d} + \frac{1}{2} \frac{\ell^3}{\ell^3} \left(\frac{(EA)_\ell}{(EA)_{b_1}} + \frac{(EA)_\ell}{(EA)_{b_2}} \right) \right]}{\left[1 + 2 \frac{a^3}{\ell^3} \frac{(EA)_\ell}{(EA)_a} + \frac{d^3}{\ell^3} \frac{(EA)_\ell}{(EA)_d} + \frac{1}{2} \frac{\ell^3}{\ell^3} \left(\frac{(EA)_\ell}{(EA)_{b_1}} + \frac{(EA)_\ell}{(EA)_{b_2}} \right) \right]}$$

$$e_4 = 0$$

$$\frac{1}{GJ} = \frac{l^2}{b^2 h^2} \frac{1}{(EA)_e} \left[1 + 2 \frac{a^3 (EA)_e}{l^3 (EA)_a} + \frac{d^3 (EA)_e}{l^3 (EA)_d} + \frac{1}{2} \frac{b^3}{l^3} \left(\frac{(EA)_e}{(EA)_{b_1}} + \frac{(EA)_e}{(EA)_{b_2}} \right) \right]$$

3.3 COMPLIANCE

The compliance of the EVATA is determined by formulating the force vector of the external loads for both upper and lower arms and, then, by applying the principle of Castigliano. For simplification, the shear terms are neglected because the truss can be regarded as a slender beam. As a further simplification, it was assumed that the external forces do not include couples. Thus, the compliance matrix can be reduced to half size. And finally, since the main interest focuses on the displacement vector at the place of the load applications, only that part of the compliance matrix was determined (see Figure 3-2). Then, each compliance, C_{ij} , is composed of contributing factors representing the influence of both bending stiffnesses, torsional stiffness, and thus, for the lower and upper arm as shown in Figure 3-3. A numerical example is presented in Table 3-1.

The transformation of the external forces from the lower to upper arm is detailed in Appendix C. Details of the Castigliano method applied to the truss are presented in Appendix D.

TABLE 3-1. COMPLIANCES AND THEIR CONTRIBUTORS (POSITION I)

ij	C_{ij}	K_{f1}	K_{u1}	$\frac{10^6}{EI_1} \{K_{f1} + K_{u1}\}$	K_{f2}	K_{u2}	$\frac{10^6}{EI_2} \{K_{f2} + K_{u2}\}$	K_{fQ}	K_{uQ}	$\frac{10^6}{EI} \{K_{fQ} + K_{uQ}\}$
11	0.2249	66.505	35.218	53.521×10^{-3}	0	0.1506	0.0253×10^{-3}	0.379	64.2	171.34×10^{-3}
12	-0.0133	0	1.499	0.788×10^{-3}	0	2.8337	0.4753×10^{-3}	-0.162	-5.330	-14.572×10^{-3}
13	0.00467	1.0844	-0.671	0.2176×10^{-3}	0	-2.003	-0.3359×10^{-3}	0	1.8057	4.791×10^{-3}
22	0.0261	0	0.1288	0.06775×10^{-3}	66.51	90.512	24.661×10^{-3}	0.069	0.44256	1.3578×10^{-3}
23	-0.0062	0	-0.1349	-0.0709×10^{-3}	0	-34.238	-5.743×10^{-3}	0	-0.14992	-0.3978×10^{-3}
33	-0.00478	0.0236	0.1871	0.11077×10^{-3}	0	27.063	4.54×10^{-3}	0	0.05079	0.1348×10^{-3}

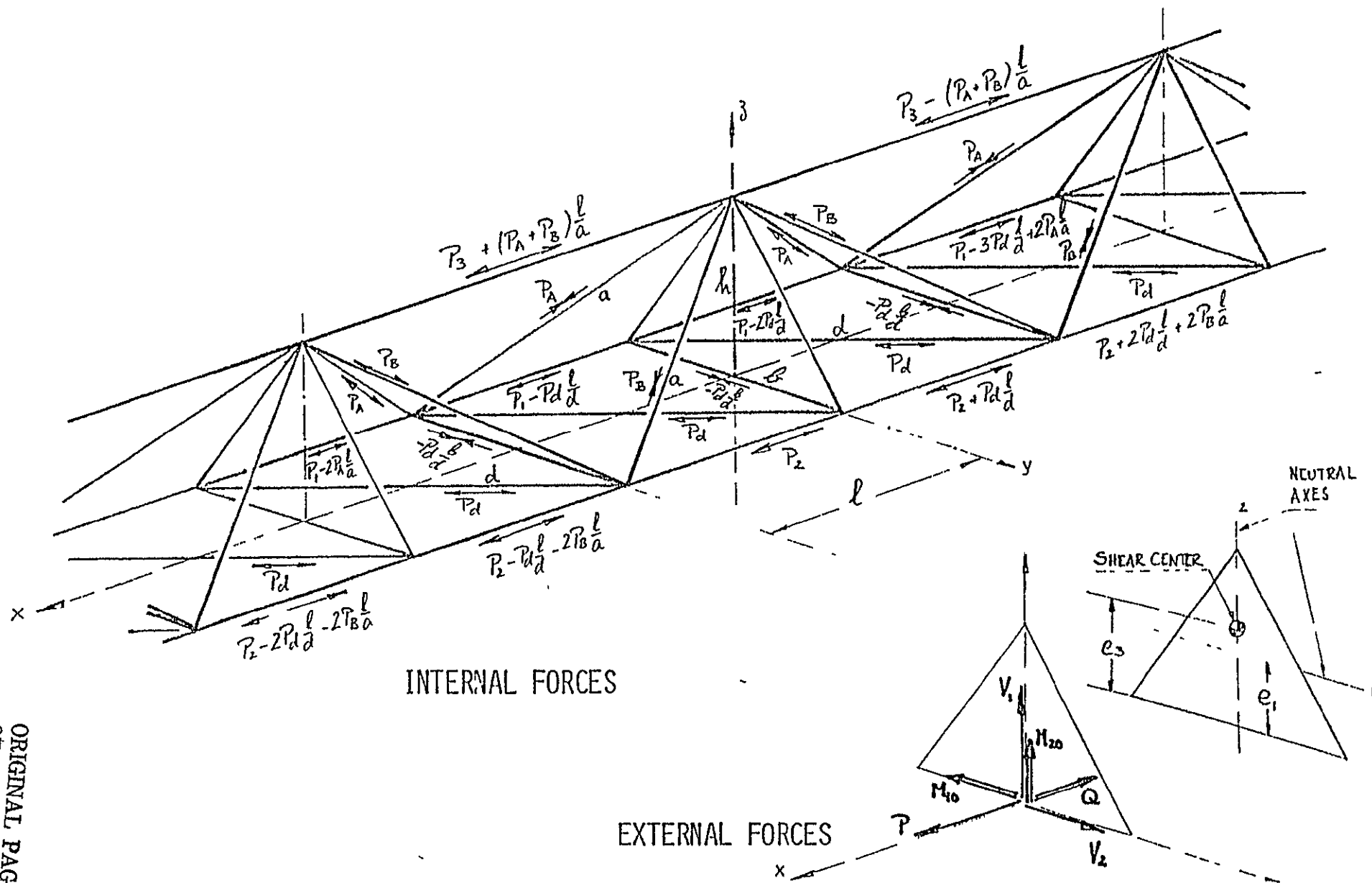


Figure 3-1. Notation of forces.

$$\begin{vmatrix} \delta_1 \\ \delta_2 \\ \delta_3 \end{vmatrix} = \begin{vmatrix} c_{11} & c_{12} & c_{13} \\ c_{21} & c_{22} & c_{23} \\ c_{31} & c_{32} & c_{33} \end{vmatrix} \times \begin{vmatrix} v_1 \\ v_2 \\ p_{\ell} \end{vmatrix}$$

Figure 3-2. General compliance matrix.

CONFIGURATION: VERTICAL LADDER MATERIAL: C/EP

$$C_{ij} = \frac{10^6}{EI_1} \left\{ K_{l1ij} + K_{u1ij} \right\} + \frac{10^6}{EI_2} \left\{ K_{l2ij} + K_{u2ij} \right\} + \frac{10^6}{GJ} \left\{ K_{\phi ij} + K_{u\phi ij} \right\}$$

$$C_1 = 6.35$$

$$C_3 = 10.884 \quad \frac{10^6}{EI_1} = 0.5289 \times 10^{-3} \quad \frac{10^6}{EI_2} = 0.16774 \times 10^{-3}$$

$$I_1 = 584.33$$

$$\frac{10^6}{GJ} = 2.653 \times 10^{-3}$$

Figure 3-3. Compliances and their contributors.

SECTION 4
APPLIED LOADS
AND RESULTING TRUSS FORCES

4.1 APPLIED LOADS

The forces and deformations were calculated for applied loads consisting of a 50-pound component in the Z-direction and 20 pounds in the X - Y plane and perpendicular to the axis of the lower arm. For the truss configuration with the face panels in a vertical position (vertical ladder), the forces are applied at a point located 6 inches above the upper longeron and in the panel plane, while for the horizontal ladder the application point lies 6 inches above the panel plane in the symmetry plane of the truss cross section (see Figure 4-1).

Several arm positions were investigated: the upper arm was kept fixed at an angle of 45 degrees away from the Orbiter X-axis and an inclination of 22.5 degrees downwards; the lower arm, with its origin 63 inches below the intersection of upper-arm axis and elbow rotary axis, was rotated forward and upwards according to the following table:

<u>Position</u>	<u>I</u>	<u>II</u>	<u>III</u>	<u>IV</u>
Out-of-plane angle between lower and upper arm	3.93°	-30°	-70°	-102.5°
Downwards inclination of lower arm	8° - 50'	6°	2° - 42'	0°
l_1	584.3	628	565	715

The distance of the load application from the elbow in the local X-axis of the lower arm, l_1 , represents the intersection of the

lower-arm axis with the symmetry plane of the Orbiter in Positions I and IV while for Positions II and III, loading points beneath the leading edge of the wing were assumed. For details see Appendix E.

4.2 FORCES AND DEFORMATIONS

The truss forces and deformations were calculated for trusses fabricated from aluminum, stainless steel, and carbon/epoxy composite tubes. The maximum forces encountered in Position I were used to determine the wall thicknesses of the members as shown in Table 4-1 and, thus, the allowable compression loads for a safety factor of 3.0 listed in Table 4-2.

Table 4-3 shows a comparison of the load capacity of the truss in its four positions as fractions of the 50-/20-pound load vector and indicates in which quadrant the applied critical force lies as defined by Figure 4-2. The magnitude of the deflection vector when the load is applied in different quadrants is shown in Table 4-4. A comparison of the margin of safety and maximum deflection for the truss in Position I is shown in Table 4-5 for various materials and lists, as well as, the corresponding truss weight.

See Appendix F for detailed load analyses and resulting truss forces and margins of safety. Appendix G is a collection of the compliance matrices, their contributing factors, and the deformations resulting from the standard forces as determined for various positions and materials. Appendix H contains the analyses for the configuration with the truss panels, horizontal rather than vertical.

TABLE 4-1. CROSS SECTIONS OF TRUSS MEMBERS

CONFIGURATION	VERTICAL LADDER			HORIZONTAL LADDER
MATERIAL	AL	CRES	G/EPOXY	G/EPOXY
MAIN SCISSOR (REAR LONGERON)				
O.D. (IN.)	1.125	1.125	1.125	1.25
I.D. (IN.)	(FULL)	0.935	0.875	0.97
A (IN ²)	0.994	0.3074	0.3927	0.4882
FRONT LONGERONS (A-FRAME, DIAGONAL, CROSS BRACES)				
O.D. (IN.)	1.125	1.125	1.125	1.25
I.D. (IN.)	0.75	0.935	0.875	1.03
A (IN ²)	0.552	0.3074	0.3927	0.3940
KNEE BRACES				
O.D. (IN.)	1.125	1.125	1.125	1.25
I.D. (IN.)	0.995	1.055	1.000	1.125
A (IN ²)	0.2165	0.1199	0.2086	0.2332
AUXILIARY SCISSOR (ACTUATOR)				
O.D. (IN.)	0.50	0.50	0.50	0.50
I.D. (IN.)	0.375	0.416	0.40	0.40
A (IN ²)	0.0859	0.06043	0.07068	0.07068
TRUSS WEIGHT, (LBS)	767	1062	392	389

TABLE 4-2. ALLOWABLE COMPRESSION LOADS FOR TRUSS MEMBERS (S.F. = 3.0)

ARM POSITION	I	II	III	IV
CRITICAL LOADING	Q ₂	Q ₄	Q ₃	Q ₃
FRACTIONAL LOAD CAPACITY WITH S.F. = 3				
VERTICAL LADDER				
ALUMINUM	1.00	0.29	0.46	0.31
GRAPHITE/EPOXY	1.27	0.40	0.65	0.44
(CRITICAL MEMBER)	LOWER NO. 2 SCISSORS	UPPER ARM DIAGONALS	UPPER ARM DIAGONALS	UPPER ARM DIAGONALS
HORIZONTAL LADDER				
GRAPHITE/EPOXY	1.05			
(CRITICAL MEMBER)	UPPER NO. 14 SCISSORS			

TABLE 4-3. SUMMARY OF FRACTIONAL LOAD CAPACITY (Pounds)

	VERTICAL LADDER		HORIZONTAL LADDER
	ALUMINUM	G/EPOXY	G/EPOXY
LONGERONS	1744	2756	3022
REAR LONGERON (SCISSOR)	543	689	894
A-FRAME MEMBER	1112	1764	1621
DIAGONALS	763	1207	1621
BATTENS	1358	2147	3496

TABLE 4-4. DEFLECTIONS (ABSOLUTE) = $\sqrt{\delta_1^2 + \delta_2^2 + \delta_3^2}$ UNDER 20/50 LOAD

Configuration	Material	Position	δ (in.) (no joint knockdown)	
			Q_1, Q_3	Q_2, Q_4
Vertical ladder	Al	I	7.20	5.23
		II	8.90	19.82
		III	26.35	30.31
		IV	49.13	48.24
	G/epoxy	I	5.35	4.00
		IV	34.62	34.46
Horizontal ladder	G/epoxy	I	3.65	2.53

TABLE 4-5. PERFORMANCE/WEIGHT COMPARISON

CONFIGURATION		VERTICAL LADDER		HORIZONTAL LADDER
MATERIAL	AL	CRES	G/EPOXY	G/EPOXY
MINIMUM MARGIN OF SAFETY (S.F.=3) IN POSITION I WITH q_2 LOAD	0.004	0.36	0.27	0.075
DISPLACEMENT AT LOADING POINT WITH q_1 LOAD (NO JOINT KNOCKDOWN)	7.20 IN.	5.26 IN.	5.35 IN.	3.65 IN.
TRUSS WEIGHT	767 LBS	1062 LBS	392 LBS	389 LBS

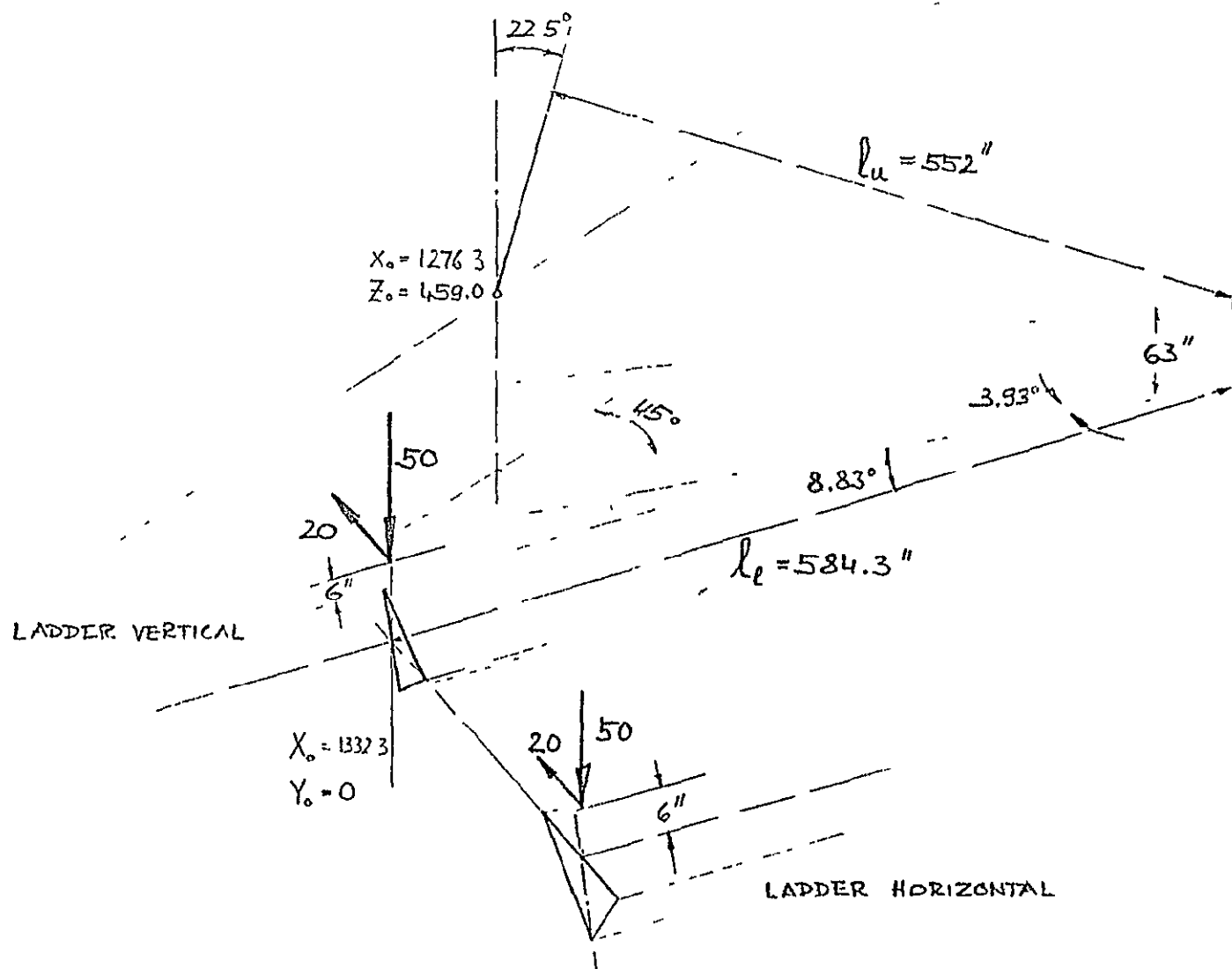
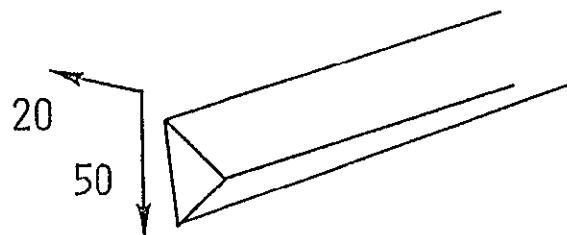


Figure 4-1. Standard applied load.

SENSE OF LOAD



50 LB IN -Z DIRECTION / 20 LB IN X-Y PLANE FORWARD

q_1 50/20 (AS ILLUSTRATED ABOVE)

q_2 50/-20

q_3 -50/-20

q_4 -50/20

Figure 4-2. Loading combinations.

SECTION 5

DEPLOYMENT

5.1 DEPLOYMENT SEQUENCE

The deployment sequence will be governed by the design of the cradle and shoulder which mount the booms to the Shuttle. The ESS was mounted at the center of its 35-foot length and deployed outward in both directions simultaneously. This is shown in Figure 1-2, Section 1. The center face hinge was hard mounted to the spacecraft and the actuating arms forced the synchronized scissor joints apart, thereby deploying the truss.

The deployment sequence envisioned for the EVATA starts with both booms and the elbow stowed and the entire package angled over at the required upper boom angle by the shoulder. The two face hinges at the end of the upper booms are hard mounted to the shoulder and the deployment mechanism, which could be a ball screw assembly, operates on the first synchronized scissor joint. The upper boom would be fully deployed and locked by an astronaut from the Shuttle bay. The spring-loaded latches in the scissors and knees will automatically lock when the boom is fully deployed. The astronaut would then translate along the upper boom to the elbow. If he wished to proceed further, he would deploy and lock the elbow. The deployment of the lower boom would be identical to the deployment of the upper boom.

5.2 DEPLOYMENT RATE

The deployment rate chosen for each boom is a tradeoff between spacecraft and boom dynamics and astronaut fatigue. Assuming enough mechanical advantage could be obtained with a small number of turns

of the deployment device, the faster deployment rate will lower the EVA time and lessen astronaut fatigue. However, the deployment of the 46- and 63-foot booms will have an impact on spacecraft dynamics and may dictate an acceptable deployment rate. Also, the faster deployment rate results in lead screw angles that have poor back-driving characteristics. This is true for most of the common devices used to convert rotary motion to linear motion. With faster deployment rates, it may be necessary to have secondary locking devices to enable the astronaut to stop in a partially deployed position.

SECTION 6

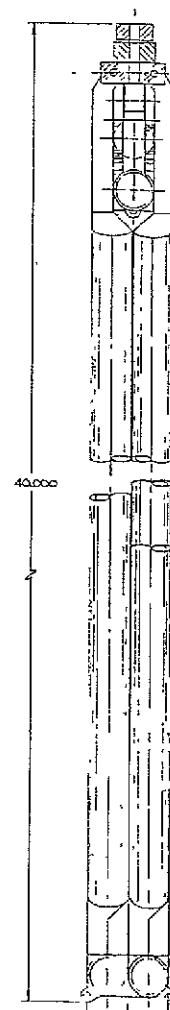
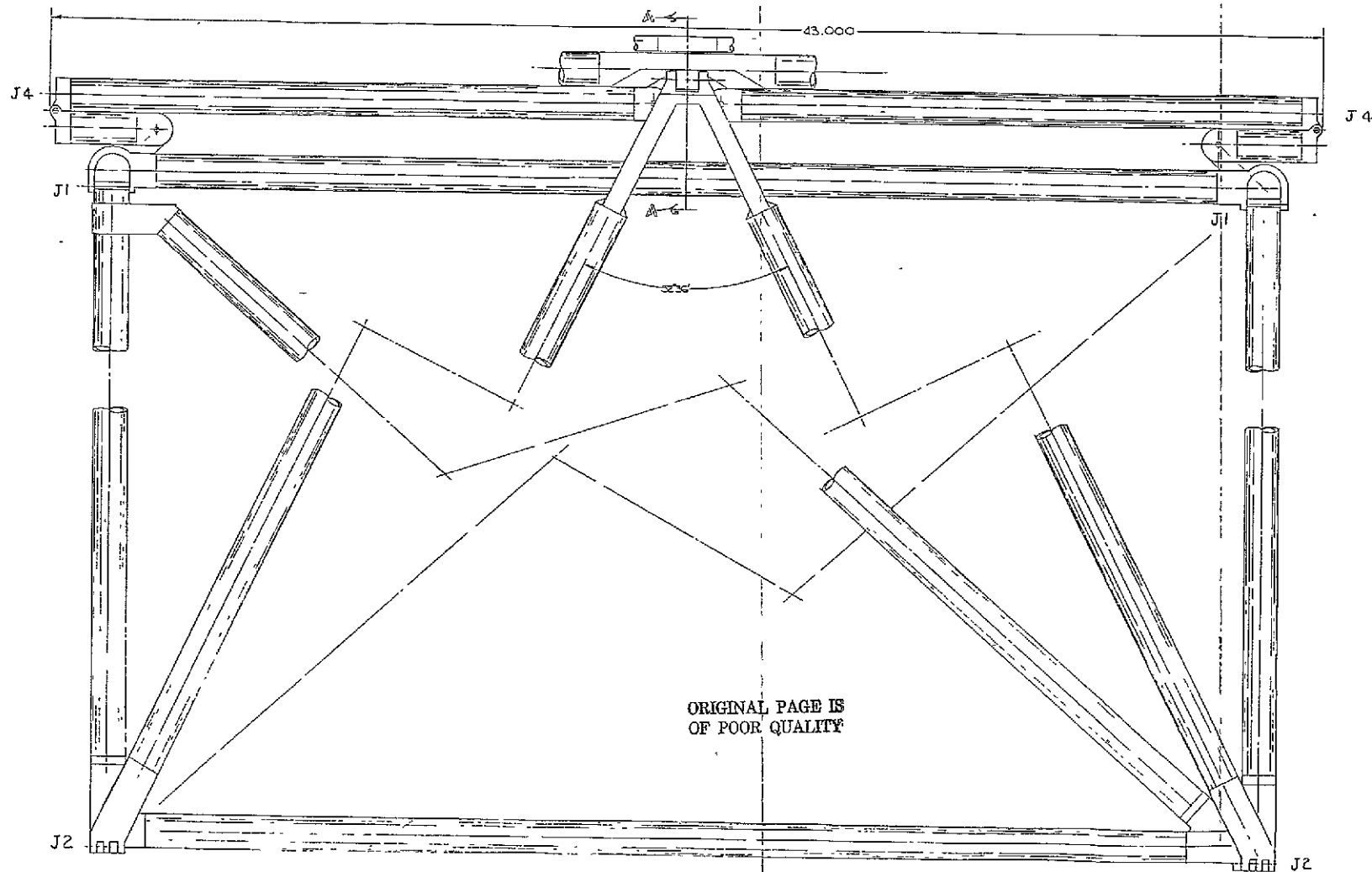
INTERFACES

6.1 ORBITER INTERFACES

The cradle and shoulder assemblies, as designed by JSC, interface directly with the Shuttle payload mounts. As described in Section 5.1, the upper boom is attached to the shoulder through the two face hinges and through the deployment actuator at the synchronized scissor joint. The configuration of the boom at the last bay can be seen in Astro SK 1958.

6.2 WORK STATION

The work station designs included in the Statement of Work (NASA-S-78-11292 and NASA-S-78-11293) were reviewed and found to be inadequate for transferring loads from the working astronaut to the truss structure efficiently. During the working sessions at NASA JSC, Astro proposed the use of a translatable roller-mounted structure which would pick up the sides of the face longerons of the truss and apply loads into the truss over four widely spaced contact points. NASA JSC has developed this concept as a preliminary design.



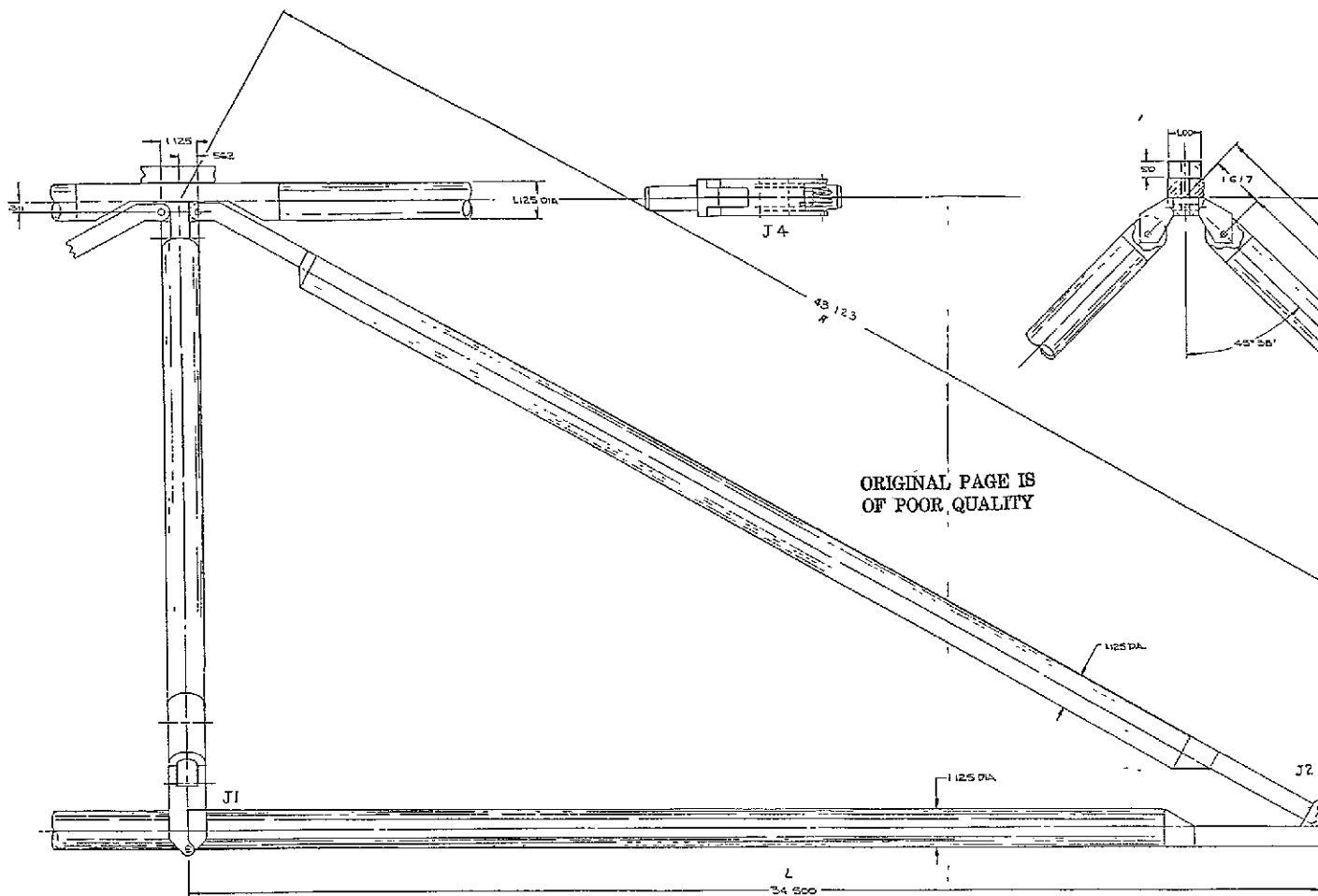
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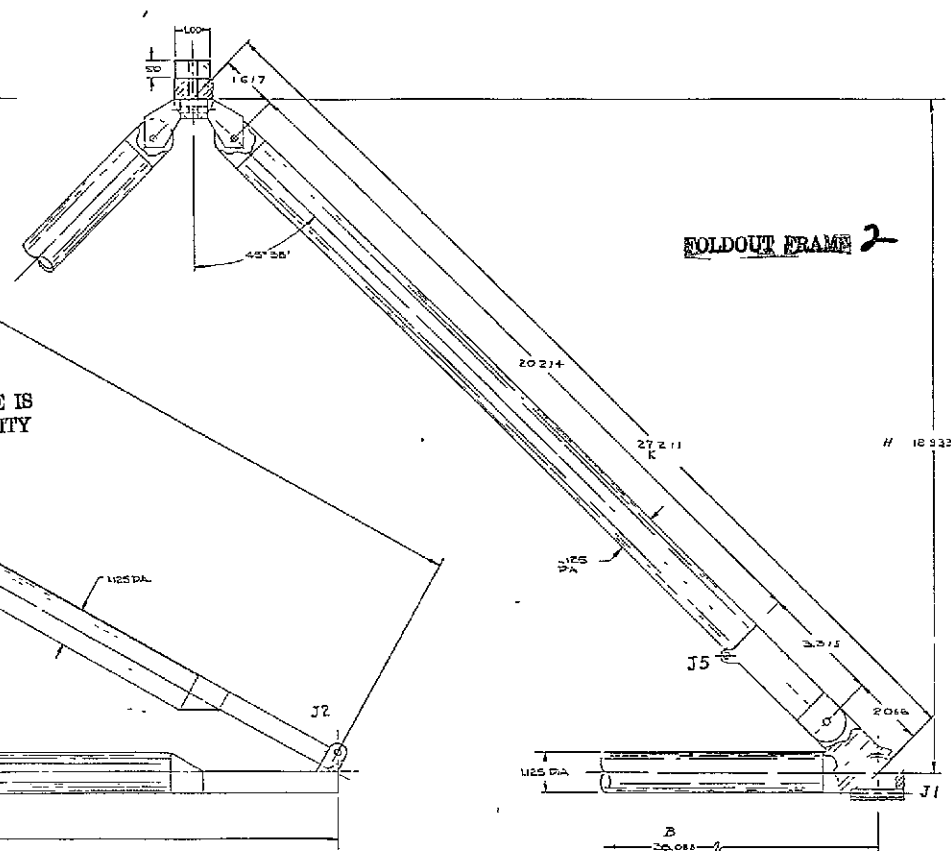
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(EVATA)
EVA TRANSLATION
RID

ASTRO
RESEARCH CORPORATION
SK 1958
A

SECTION 7

RETRACTION AND JETTISON

7.1 RETRACTION

The ESS, as developed and flown on SEASAT, is required to deploy only. The latches and the spring-loaded hinges were designed to deploy and lock. The EVATA structure has to retract as well as deploy. For retraction, the spring-loaded knee hinges and the spring-biased scissor latches have to be forced open. Figures 7-1 and 7-2 show the ESS latches and joints. Rather than add secondary mechanisms to force the hinges and latches open, Astro investigated using the existing synchronizer assembly (see Figure 7-3) to initiate and control the retraction. In the ESS, the synchronized scissor joint controls the deployment of each bay of the truss by operating on the A-frame assembly through a linkage system with a fixed relationship between scissor rotation and A-frame angle. If the synchronizer attachment point is moved from the A-frame to the knee strut, a reversal of scissor force will act to force open the spring-loaded knee hinges directly. The synchronizer linkage arrangement for the ESS was tailored to match the relationship between the A-frame angle and the scissor angle. Appendix I shows the knee brace synchronizer analysis necessary to tailor the rotation of the scissors to the required knee strut angle. The analysis was performed early in the program before the kinematic analysis determined the final dimensions for panel length and truss depth. The numbers chosen, while different from the proposed design, indicate the shape of the required synchronizer curve and the equations which were set up apply to the final design as proposed.

Astro has modified the half-scale ESS model with a knee brace synchronizer of the type proposed. The model proved the concept

of initiating and controlling the retraction. The accuracy of synchronizing with the knee brace synchronizer was not determined due to the use of existing components which prevented the use of the ideal theoretical linkage dimensions.

7.2 JETTISON

The jettison problem was not considered as part of this study due to the jettison plane being moved to the NASA JSC portion of the structure.



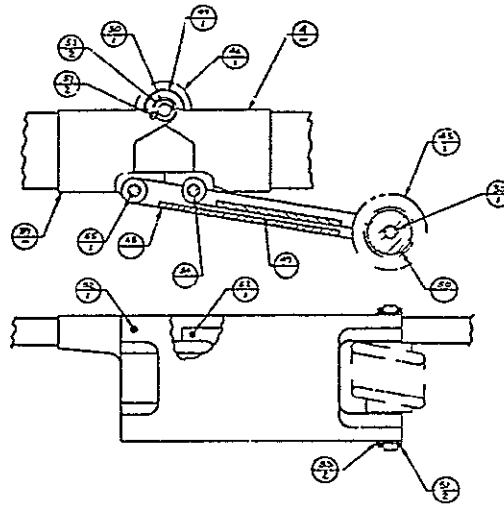


Figure 7-2. Longeron hinge.

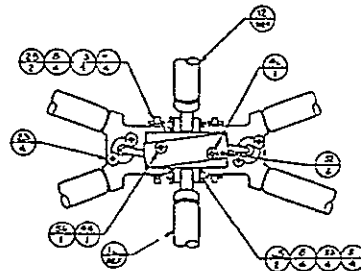
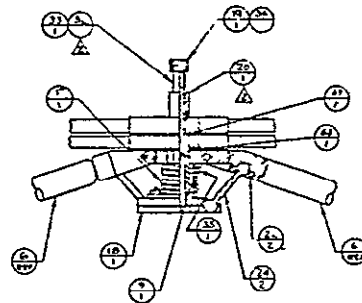


Figure 7-3. Synchronized joint.

SECTION 8

DEVELOPMENT PLAN AND SCHEDULE

8.1 PRELIMINARY MATERIAL SELECTION

The only truss material analyzed which meets the baseline requirements for weight (400 pounds) and deflection (6-inch system deflection at ET door) is graphite/epoxy tube. Aluminum alloy fittings were chosen due to cost and schedule advantages over titanium fittings. The materials combination used on the SEASAT ESS were graphite/epoxy tube and titanium fittings. The joints would be bonded using techniques developed on the SEASAT and JPL Voyager programs.

8.2 GRAPHITE/EPOXY EXPERIENCE

Astro Research Corporation has flight system experience on the SEASAT program and has successfully completed programs for the development of bonded joints between graphite/epoxy tubes and titanium fittings. The SEASAT program also included in-house preparation and control of graphite/epoxy tube material procurement, fabrication, and bonding specifications.

Through in-house Research and Development programs, Astro developed experimental Astromasts using in-house fabricated graphite/epoxy longerons. Table 8-1 summarizes the major parameters controlled by the graphite/epoxy procurement specifications.

8.3 INDUSTRY EXPERIENCE - GRAPHITE/EPOXY/ALUMINUM ALLOY FITTINGS

NASA JPL concluded a development program with the selection of graphite/epoxy tube and aluminum alloy fittings as the main structural members for the Voyager science boom and the antenna support

structure. As part of the Voyager development program, JPL developed a bonded joint using a fiberglass interliner to compensate for the different thermal expansion between aluminum and graphite/epoxy. The joint was qualified by comparing room temperature joint strength before and after plunging the joints in LN_2 .

8.4 REQUIRED EVATA COMPONENT DEVELOPMENT TESTS

Using the development history of the SEASAT ESS as a guide, the list of component development tests shown on Table 8-2 was generated. All the tests listed would be performed by Astro except the thermal coating evaluation.

8.5 REQUIRED EVATA SYSTEM TESTS

Table 8-3 shows the system tests required for the full-scale model and the flight deliverable EVATA. The full-scale model tests would be performed at Astro. The flight deliverable environmental testing and the deployment and retraction on an air bearing floor would be at NASA JSC.

8.6 SCHEDULE

The program schedule in Figure 8-1 shows a 24-week development program and a 14-week flight hardware production program. This program schedule was generated using the SEASAT development and production program as a guide.

TABLE 8-1. SEASAT A ESS
GRAPHITE/EPOXY COMPOSITE SPECIFICATIONS

TUBING

DIAMETER:	0.500 IN \pm 0.005 IN.
WALL THICKNESS (APPROX.):	0.030 IN.
LENGTH:	72 IN. \pm 3 IN.
ROUNDNESS (WITHIN):	0.005 IN. ON DIAMETER
Bow:	LESS THAN 0.1 IN. OVER 6 FT

STRIP

RECTANGULAR CROSS SECTION:	0.25 IN. X 0.75 IN.
FLATNESS:	LESS THAN 0.03 IN.

MECHANICAL PROPERTIES

TENSILE MODULUS:	$>15 \times 10^6$ PSI
------------------	-----------------------

THERMAL PROPERTIES

COEFFICIENT OF THERMAL EXPANSION:	$\pm 0.5 \times 10^{-6}$ IN/IN/ $^{\circ}$ F
--------------------------------------	--

<u>VOID CONTENT:</u>	<1%
----------------------	-----

TABLE 8-2. EVATA REQUIRED COMPONENT DEVELOPMENT TESTS

• HINGE DEVELOPMENT

500 CYCLES UNDER LOAD FOR WEAR

• GRAPHITE/EPOXY ALUMINUM BOND JOINT TESTS

- BONDS FOR NOMINAL STRENGTH
- BONDS FOR DEGRADATION AFTER THERMAL SHOCK

• SINGLE BAY MODEL (INCLUDING DEPLOYMENT ACTUATOR)

- DEPLOYMENT TESTS
- ORIENTATION AND ALIGNMENT TESTS
- OPERATION IN THERMAL VACUUM CHAMBER

• SYNCHRONIZER MODEL TESTS

- SYNCHRONIZATION
- MECHANICAL EFFICIENCY

• THERMAL COATING EVALUATION (JSC)

TABLE 8-3. REQUIRED EVATA SYSTEM TESTS

- FULL SCALE MODEL TESTS - LOWER ARM
 - DEPLOYMENT AND RETRACTION, 1g - AIR BEARING SUPPORTED
 - ORIENTATION AND ALIGNMENT
 - COMPLIANCE
 - WEIGHT AND CENTER OF GRAVITY - STOWED
 - NATURAL FREQUENCY
 - CENTER OF GRAVITY - DEPLOYED

- FLIGHT DELIVERABLE - EVATA
 - LAUNCH AND BOOST, VIBRATION, AND ACCELERATION - STOWED
 - DEPLOYMENT AND RETRACTION, 1g - AIR BEARING SUPPORTED
 - SYSTEM WEIGHT AND CENTER OF GRAVITY - STOWED

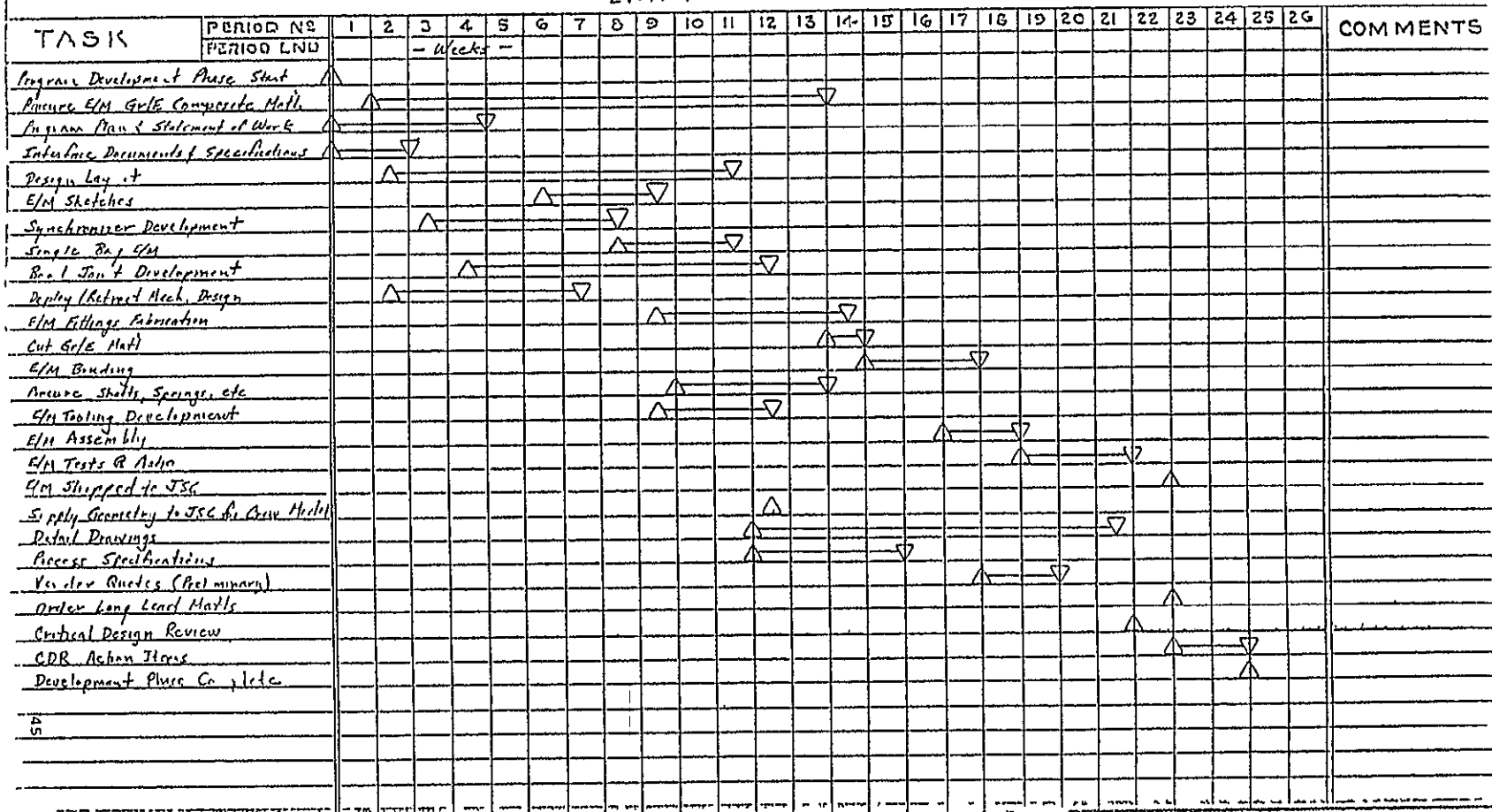
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SANTA BARBARA, CALIF. 6117-a
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Figure 8-1 Program schedule.

- EVATA -



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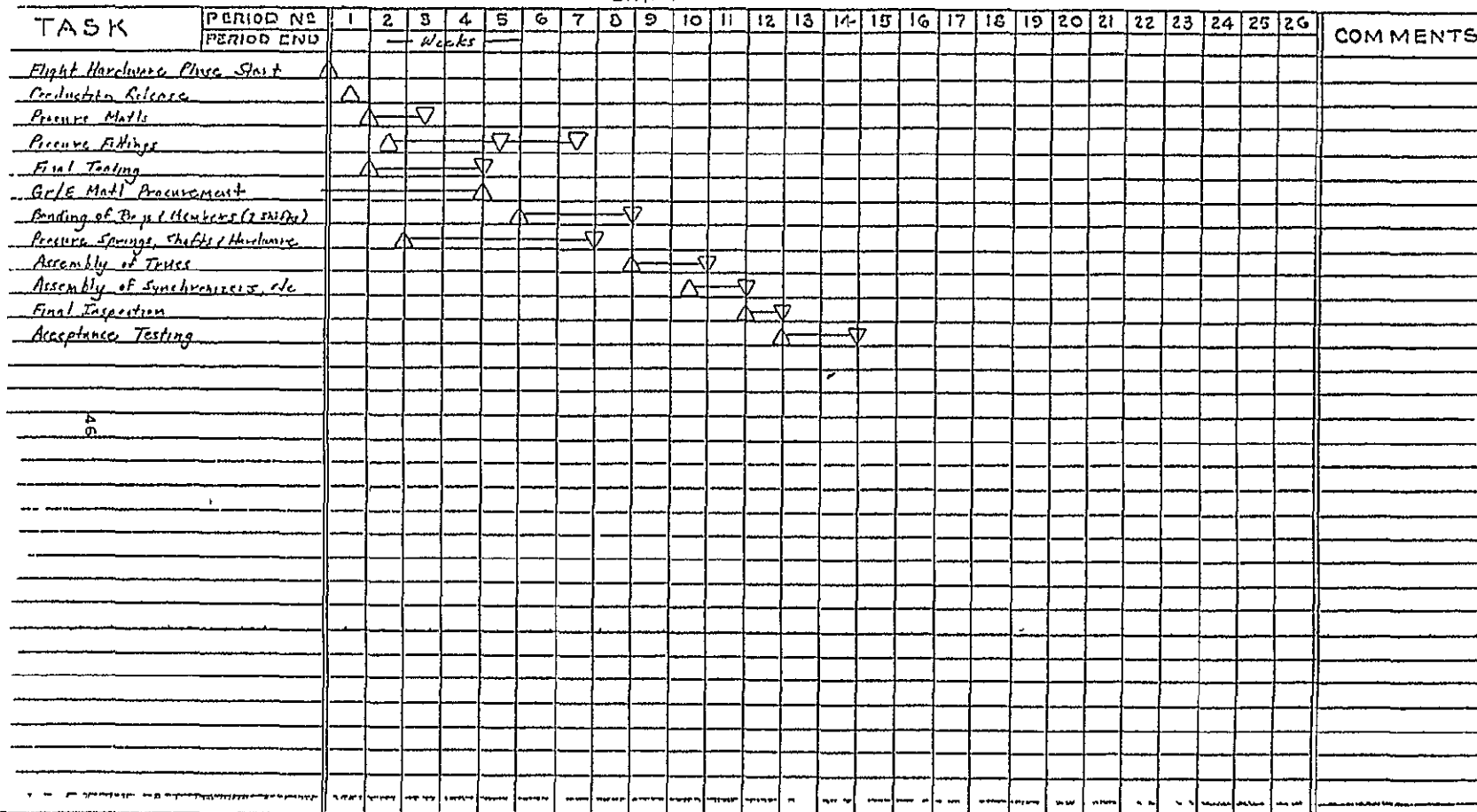
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SANTA BARBARA, CALIF.

Figure 8-1 Continued

- EVATA -



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SECTION 9

EVATA COSTS

Table 9-1 details the budgetary cost estimate for each phase of the EVATA development and production program. It also gives a comparison of costs using graphite/epoxy tubing or aluminum tubing as the basic truss material.

TABLE 9-1. ESTIMATED EVATA PROGRAM COSTS

PHASE I	DESIGN, DEVELOPMENT, FABRICATION, AND TESTING OF ENGINEERING MODEL UNIT	
	A. USING GRAPHITE/EPOXY TUBING (INCLUDES PROCUREMENT OF GRAPHITE/EPOXY FOR FLIGHT HARDWARE)	\$1,075,801
	B. USING ALUMINUM TUBING	418,654
PHASE II	FABRICATION AND TEST OF FLIGHT UNIT	
	A. USING GRAPHITE/EPOXY TUBING (PURCHASED IN PHASE I)	278,654
	B. USING ALUMINUM TUBING	285,039
TOTAL PROGRAM COSTS, GRAPHITE/EPOXY TUBING		1,354,455
TOTAL PROGRAM COSTS, ALUMINUM TUBING		703,693

SECTION 10

CONCLUSIONS AND RECOMMENDATIONS

The primary purpose of this study contract was to perform a preliminary design of a deployable structure to allow an astronaut to perform tasks in the vicinity of the ET umbilical doors. As a secondary goal, the EVATA allows inspection of the entire underside of the Shuttle spacecraft. This secondary goal requires that the boom lengths be increased to reach the ET doors from the center of the spacecraft. As shown in the analysis sections of this report, the length of the booms is the major driver in terms of system weight and cost. Because of this length effect, the secondary function of the EVATA has dictated a very large and expensive structure.

If the system was designed solely for the primary function of ET door inspection and repair, the original NASA JSC concept of using two short arms over the trailing edge of the wing is the optimum from a standpoint of weight and cost. Going over the trailing edge of the wing results in deployable booms similar in length to the SEASAT A ESS.

It is Astro's recommendation that the original concept of going over the trailing edge be investigated to fulfill the primary mission of ET door inspection and repair. A rough-order-of-magnitude analysis shows that an all aluminum deployable truss-type structure can be designed and built within the weight and cost budgets of 800 pounds and \$500,000, respectively. This would include upper and lower booms, the elbow, and all the structure necessary to mount the booms to the Shuttle keel and longeron payload mounting points. The entire

structure would stow within the last 48 inches of the Shuttle payload bay. The design, fabrication, and testing of this structure could be handled entirely by Astro with little or no impact on NASA JSC in-house programs and personnel.

APPENDIX A

RELATIONS BETWEEN INTERNAL AND EXTERNAL FORCES

Relations between Internal and External Forces

$$\begin{aligned}
 P_1 - \frac{l}{d} P_d + P_2 + P_3 + \frac{l}{a} (P_2 + P_3) + \frac{l}{d} P_d - \frac{l}{a} (P_A - P_B) &= P \\
 - \frac{l}{d} P_d + \frac{l}{2a} (P_A - P_B) &= V_2 \\
 \frac{l}{a} (P_A + P_B) &= V_1 \\
 \frac{bl}{2a} (P_A - P_B) &= Q \\
 - \left(P_3 + \frac{l}{a} (P_A + P_B) \right) h - \frac{l}{a} (P_A + P_B) \frac{1}{2} \left(1 - \frac{v}{\ell} \right) &= M_1 = M_{10} - V_1 x \\
 (P_1 - \frac{l}{d} P_d - P_2) \frac{h}{2} - \frac{1}{d} \frac{bl}{2} \left(1 - \frac{v}{\ell} \right) - \frac{l}{a} (P_A - P_B) \frac{1}{2} \frac{x}{\ell} &= M_2 = M_{20} - V_2 x
 \end{aligned}$$

Thus,

$$P_1 + P_2 + P_3 = P$$

$$- \frac{l}{d} P_d + \frac{l}{2a} (P_A - P_B) = V_2$$

$$\frac{l}{a} (P_A + P_B) = V_1$$

$$\frac{bl}{2a} (P_A - P_B) = Q$$

$$- P_3 h = M_{1c}$$

$$(P_1 - P_2) \frac{h}{2} - \frac{bl}{d} P_d = M_{20}$$

Then,

$$- \frac{l}{d} P_d = V_2 - \frac{Q}{h}$$

$$\text{or } P_d = \frac{d}{l} \left(\frac{Q}{h} - V_2 \right)$$

$$P_3 = - \frac{M_{1c}}{h}$$

$$P_1 - P_2 = P + \frac{H_{10}}{h}$$

$$P_1 - P_2 = \frac{2}{b} \left[H_{20} + \ell \left(\frac{Q}{h} - V_2 \right) \right]$$

$$P_A - P_B = \frac{2a}{bh} Q$$

$$P_A + P_B = \frac{a}{h} V_1$$

$$P_1 = \frac{P}{2} + \frac{H_{10}}{2h} + \frac{H_{20}}{b} + \frac{\ell}{bh} Q - \frac{\ell}{b} V_2$$

$$P_2 = \frac{P}{2} + \frac{H_{10}}{2h} - \frac{H_{20}}{b} - \frac{\ell}{bh} Q + \frac{\ell}{b} V_2$$

$$P_A = \frac{a}{2h} V_1 + \frac{a}{bh} Q$$

$$P_B = \frac{a}{2h} V_1 - \frac{a}{bh} Q$$

Now, for S E

$$2P_1^2 + 2P_2^2 = \left(P + \frac{H_{10}}{h} \right)^2 + \left(\frac{2H_{20}}{b} + \frac{2\ell}{bh} Q - 2 \frac{\ell}{b} V_2 \right)^2$$

$$\text{and } 2P_A^2 + 2P_B^2 = \left(\frac{2a}{bh} Q \right)^2 + \left(\frac{a}{h} V_1 \right)^2$$

APPENDIX B

CHARACTERIZATION OF TRUSS BY CONTINUOUS BEAM

Characterization of Truss by Continuous Beam

Strain Energy for length $2l$

1 Truss

$$\begin{aligned}
 SE / \text{module} &= \frac{l}{2(EA)_1} \left[\left(P_1 - \frac{l}{d} P_d \right)^2 + \left(P_1 - 2 \frac{l}{d} P_d \right)^2 + P_2^2 + \left(P_2 + \frac{l}{d} P_d \right)^2 \right] \\
 &+ \frac{l}{2(EA)_2} \left[\left(P_3 + \frac{l}{a} (P_A + P_B) \right)^2 + \left(P_3 - \frac{l}{a} (P_A + P_B) \right)^2 \right] \\
 &+ \frac{a}{2(EA)_a} \left[2 P_A^2 + 2 P_B^2 \right] \\
 &+ \frac{d}{2(EA)_d} 2 P_d^2 \\
 &+ \frac{l}{2(EA)_{l_1}} \left[\frac{l}{d} P_d \right]^2 \\
 &+ \frac{l}{2(EA)_{l_2}} \left[\frac{l}{d} P_d \right]^2
 \end{aligned}$$

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$$\begin{aligned}
 &= \frac{l}{2(EA)_1} \left[2 P_1^2 - 6 \frac{l}{d} P_1 P_d + 6 \left(\frac{l}{d} \right)^2 P_d^2 + 2 P_2^2 + 2 \frac{l}{d} P_2 P_d \right] \\
 &+ \frac{l}{2(EA)_2} \left[2 P_3^2 - 2 \left(\frac{l}{a} \right)^2 (P_A + P_B)^2 \right] \\
 &- \frac{a}{2(EA)_a} \left[2 P_A^2 + 2 P_B^2 \right] \\
 &+ \frac{d}{2(EA)_d} 2 P_d^2 \\
 &+ \frac{l}{2} \left(\frac{1}{(EA)_{l_1}} + \frac{1}{(EA)_{l_2}} \right) \left(\frac{l}{d} \right)^2 P_d^2
 \end{aligned}$$

$$S E / \text{module} = \frac{l}{2(EA)_l} \left[\left(P + \frac{H_{10}}{l} \right)^2 + \left(\frac{2H_{20}}{b} + \frac{2l}{bl} Q - 2 \frac{l}{b} V_2 \right)^2 + 6 \left(\frac{l}{b} \right)^2 \left(\frac{Q}{l} - V_2 \right)^2 \right.$$

$$+ 2 \frac{l}{b} \left(\frac{Q}{l} - V_2 \right) \left(\frac{P}{2} + \frac{H_{10}}{2l} - \frac{H_{20}}{b} - \frac{l}{bl} Q - \frac{l}{b} V_2 \right) \\ \left. - 3 \frac{P}{2} - 3 \frac{H_{10}}{2l} - 3 \frac{H_{20}}{b} - 3 \frac{l}{bl} Q + 3 \frac{l}{b} V_2 \right]$$

$$+ \frac{l}{2(EA)_s} \left[2 \frac{H_{10}^2}{l^2} + 2 \frac{l^2}{b^2} V_2^2 \right]$$

$$+ \frac{a}{2(EA)_a} \left[4 \frac{a^2}{b^4 l^2} Q^2 + \frac{a^2}{l^2} V_1^2 \right]$$

$$+ \frac{d}{2(EA)_d} \left[2 \frac{d^2}{b^2} \left(\frac{Q}{l} - V_2 \right)^2 \right]$$

$$+ \frac{l}{2} \left(\frac{1}{(EA)_{b_1}} + \frac{1}{(EA)_{b_2}} \right) \left(\frac{Q}{l} - V_2 \right)^2$$

$$= \frac{l}{2(EA)_l} \left[P^2 + \frac{H_{10}^2}{l^2} + 4 \frac{H_{20}^2}{b^2} + 4 \frac{l^2}{b^4 l^2} Q^2 + 4 \frac{l^2}{b^2} V_2^2 + 2 P \frac{H_{10}}{l} + 8 \frac{l}{b^2 l} H_{20} Q - 8 \frac{l}{b^2} H_{20} V_2 - 8 \frac{l^2}{b^2 l} Q V_2 \right.$$

$$+ 6 \frac{l^2}{b^4 l^2} Q^2 + 6 \frac{l^2}{b^2} V_2^2 - 12 \frac{l^2}{b^4 l} Q V_2$$

$$- 8 \frac{l^2}{b^4 l^2} Q^2 - 8 \frac{l^2}{b^2} V_2^2 - 8 \frac{l}{b^2 l} H_{20} Q + 8 \frac{1}{l^2} H_{20} V_2 + 16 \frac{l^2}{b^4 l}$$

$$- 2 \frac{l}{b^4 l} P Q - 2 \frac{l}{b^4 l^2} H_{10} Q + 2 \frac{l}{b^4 l} V_2 H_{10} + 2 \frac{l}{b} P V_2$$

+

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$$S E / module = M_{10}^2 \left(\frac{l}{2l^2(EA)_e} + \frac{l}{l^2(EA)_s} \right)$$

$$+ M_{20}^2 \frac{2l}{l^2(EA)_e}$$

$$+ Q^2 \left[\frac{l^3}{l^2 l^2 (EA)_e} + 2 \frac{a^3}{l^2 l^2 (EA)_a} + \frac{d^3}{l^2 l^2 (EA)_d} + \frac{l^3}{l^2 l^2 2} \left(\frac{1}{(EA)_{b_1}} + \frac{1}{(EA)_{b_2}} \right) \right]$$

$$+ P^2 \frac{l}{2(EA)_e}$$

$$+ V_1^2 \left[\frac{l^3}{l^2 (EA)_s} + \frac{1}{2} \frac{a^3}{l^2 (EA)_e} \right]$$

$$+ V_2^2 \left[\frac{l^3}{l^2 (EA)_e} + \frac{d^3}{l^2 (EA)_d} + \frac{l}{2} \left(\frac{1}{(EA)_{b_1}} + \frac{1}{(EA)_{b_2}} \right) \right]$$

$$+ P M_{10} \frac{l}{l (EA)_e}$$

$$+ P Q \frac{l^2}{l l (EA)_e}$$

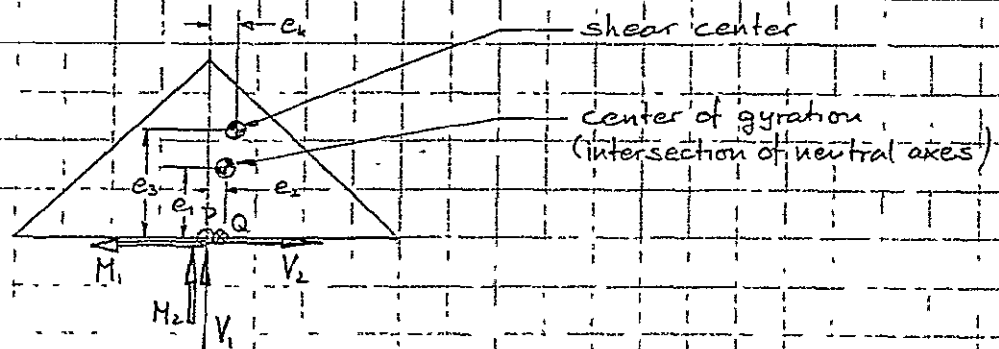
$$+ P V_2 \frac{l^2}{l (EA)_e}$$

$$+ V_2 M_{10} \frac{l^2}{l l (EA)_e}$$

$$- V_2 Q \left[2 \frac{l^3}{l^2 l (EA)_e} + 2 \frac{d^3}{l^2 l (EA)_d} + \frac{l}{l l} \left(\frac{1}{(EA)_{b_1}} + \frac{1}{(EA)_{b_2}} \right) \right]$$

$$- M_{10} Q \frac{l^2}{l l^2 (EA)_e}$$

2. Equivalent Continuous Beam



$$SE/2l = \frac{1}{2} \int_{-l}^l dx \left[\frac{(M_{10} - V_1 x + P e_1)^2}{EI_1} + \frac{(M_{20} - V_2 x + P e_2)^2}{EI_2} + \frac{(Q + V_1 e_1 - V_2 e_3)^2}{GJ} \right. \\ \left. + \frac{P^2}{EA} + \frac{V_1^2}{GA_{S1}} + \frac{V_2^2}{GA_{S2}} + \text{'asymmetrical' terms} \right]$$

$$= \int \left\{ \frac{(M_{10} + P e_1)^2}{EI_1} + \frac{l^2 V_1^2}{3 EI_1} + \frac{(M_{20} + P e_2)^2}{EI_2} + \frac{l^2 V_2^2}{3 EI_2} + \frac{(Q + V_1 e_1 - V_2 e_3)^2}{GJ} \right. \\ \left. + \frac{P^2}{EA} + \frac{V_1^2}{GA_{S1}} + \frac{V_2^2}{GA_{S2}} + \text{'asymmetrical' terms} \right\}$$

$$= M_{10}^2 \frac{l}{EI_1} + M_{20}^2 \frac{l}{EI_2} + Q^2 \frac{l}{GJ} + P M_{10} \frac{2 l e_1}{EI_1} + P M_{20} \frac{2 l e_2}{EI_2}$$

$$+ P^2 \left(\frac{e_1^2 l}{EI_1} + \frac{e_2^2 l}{EI_2} + \frac{l}{EA} \right)$$

$$+ V_1^2 \left(\frac{l^3}{3 EI_1} + \frac{l}{GA_{S1}} + \frac{l e_1^2}{GJ} \right)$$

$$+ V_2^2 \left(\frac{l^3}{3 EI_2} + \frac{l}{GA_{S2}} + \frac{l e_2^2}{GJ} \right)$$

$$+ V_1 Q \frac{2 l e_1}{GJ} - V_2 Q \frac{2 l e_3}{GJ} - V_1 V_2 \frac{2 l e_3 e_1}{GJ} + \text{'asymmetric' terms}$$

3. Comparison of Terms Truss \longleftrightarrow Equivalent Beam

$$H_{10}^2 \quad \frac{l}{h^2} \left(\frac{1}{2(EA)_t} + \frac{1}{(EA)_1} \right) = \frac{l}{EI_1} \quad \text{ORIGINAL PAGE IS OF POOR QUALITY}$$

$$H_{20}^2 \quad \frac{2l}{b^2} \frac{1}{(EA)_t} = \frac{l}{EI_2}$$

$$Q^2 \quad \frac{l^3}{b^2 h^2} \left[\frac{1}{(EA)_t} + 2 \frac{a^3}{l^3} \frac{1}{(EA)_a} + \frac{d^3}{l^3} \frac{1}{(EA)_d} + 2 \frac{b^3}{l^3} \left(\frac{1}{(EA)_{b_1}} + \frac{1}{(EA)_{b_2}} \right) \right] = \frac{l}{GJ}$$

$$PH_{10} \quad \frac{l}{h(EA)_t} = \frac{2le_1}{EI_1}$$

$$PH_{20} \quad 0 = \frac{2le_2}{EI_2}$$

$$P^2 \quad \frac{l}{2(EA)_t} = l \left(\frac{e_1^2}{EI_1} + \frac{e_2^2}{EI_2} + \frac{1}{EA} \right)$$

$$V_1^2 \quad \frac{l^3}{h^2} \left(\frac{1}{(EA)_s} + \frac{1}{2} \frac{a^3}{l^3} \frac{1}{(EA)_a} \right) = l \left(\frac{l^2}{3EI_1} + \frac{1}{GA_s} + \frac{e_1^2}{GJ} \right)$$

$$V_2^2 \quad \frac{l^3}{b^2} \left(\frac{1}{(EA)_t} + \frac{d^3}{l^3} \frac{1}{(EA)_d} + \frac{1}{2} \frac{b^3}{l^3} \left(\frac{1}{(EA)_{b_1}} + \frac{1}{(EA)_{b_2}} \right) \right) = l \left(\frac{l^2}{3EI_2} + \frac{1}{GA_s} + \frac{e_2^2}{GJ} \right)$$

$$V_1 Q \quad 0 = \frac{2le_1}{GJ}$$

$$V_2 Q \quad 2 \frac{l^3}{b^2 h} \left[\frac{1}{(EA)_t} + \frac{d^3}{l^3} \frac{1}{(EA)_d} + \frac{1}{2} \frac{b^3}{l^3} \left(\frac{1}{(EA)_{b_1}} + \frac{1}{(EA)_{b_2}} \right) \right] = 2 \frac{le_2}{GJ}$$

$$V_1 V_2 \quad 0 = -2 \frac{le_1 e_2}{GJ}$$

Thus,

$$\frac{1}{EI} = \frac{1}{h^4} \left(\frac{1}{2(EA)_c} + \frac{1}{(EA)_s} \right)$$

$$\frac{1}{EI_2} = \frac{2}{b^3} \frac{1}{(EA)_c}$$

$$\frac{1}{GJ} = \frac{l^2}{b^2 h^4 (EA)_c} \left[1 + 2 \frac{a^3 (EA)_c}{l^3 (EA)_a} + \frac{d^3 (EA)_c}{l^3 (EA)_d} + \frac{1}{2} \frac{b^3}{l^3} \left(\frac{(EA)_c}{(EA)_{b_1}} + \frac{(EA)_c}{(EA)_{b_2}} \right) \right]$$

$$e_1 = \frac{EI_1}{2l(EA)_c} = \frac{h}{2} \frac{(EA)_c}{\left(\frac{1}{2(EA)_c} + \frac{1}{(EA)_s} \right)} = h \frac{1}{\left(1 + 2 \frac{(EA)_c}{(EA)_s} \right)}$$

$$e_2 = 0$$

$$\frac{1}{EA} = \frac{1}{2(EA)_c} - \frac{e_1^2}{EI_1} = \frac{1}{2(EA)_c} - \frac{h^2}{\left(1 + 2 \frac{(EA)_c}{(EA)_s} \right)^2} \frac{1}{\frac{h}{2(EA)_c} \left(1 + 2 \frac{(EA)_c}{(EA)_s} \right)}$$

$$= \frac{1}{2(EA)_c} \left(1 - \frac{1}{1 + 2 \frac{(EA)_c}{(EA)_s}} \right) = \frac{1}{(EA)_s + 2(EA)_c}$$

$$e_3 = \frac{\frac{l^2}{b^2 h^4 (EA)_c} \left[1 - \frac{d^3 (EA)_c}{l^3 (EA)_d} + \frac{1}{2} \frac{b^3}{l^3} \left(\frac{(EA)_c}{(EA)_{b_1}} + \frac{(EA)_c}{(EA)_{b_2}} \right) \right]}{\frac{l^2}{b^2 h^4 (EA)_c} \left[1 + 2 \frac{a^3 (EA)_c}{l^3 (EA)_a} + \frac{d^3 (EA)_c}{l^3 (EA)_d} + \frac{1}{2} \frac{b^3}{l^3} \left(\frac{(EA)_c}{(EA)_{b_1}} + \frac{(EA)_c}{(EA)_{b_2}} \right) \right]}$$

$$= h \frac{\left[1 - \frac{d^3 (EA)_c}{l^3 (EA)_d} + \frac{1}{2} \frac{b^3}{l^3} \left(\frac{(EA)_c}{(EA)_{b_1}} + \frac{(EA)_c}{(EA)_{b_2}} \right) \right]}{\left[1 + 2 \frac{a^3 (EA)_c}{l^3 (EA)_a} + \frac{d^3 (EA)_c}{l^3 (EA)_d} + \frac{1}{2} \frac{b^3}{l^3} \left(\frac{(EA)_c}{(EA)_{b_1}} + \frac{(EA)_c}{(EA)_{b_2}} \right) \right]}$$

$$e_4 = 0$$

abbreviations $\frac{a^3 (EA)_e}{l^3 (EA)_a} = k_a$

$$\frac{d^3 (EA)_d}{l^3 (EA)_d} = k_d$$

$$\frac{b^3 \left(\frac{(EA)_e}{(EA)_b} + \frac{(EA)_c}{(EA)_l} \right)}{l^3} = k_b$$

$$\frac{(EA)_s}{(EA)_s} = k_s$$

then,

$$\frac{1}{GA_{s1}} = \frac{l^2}{l^2} \left(\frac{1}{(EA)_s} + \frac{1}{2} \frac{a^3}{l^3} \frac{1}{(EA)_a} \right) - \frac{l^2}{3EI_1} = \frac{l^2}{l^2 (EA)_e} \left[k_s + \frac{1}{2} k_a - \frac{1}{6} - \frac{1}{3} k_s \right]$$

$$= \frac{l^2}{6 l^2 (EA)_e} [4 k_s + 3 k_a - 1]$$

$$\frac{1}{GA_{s2}} = \frac{l^2}{b^2 (EA)_e} \left[1 + k_d + \frac{1}{2} k_b \right] - \frac{l^2}{3EI_2} - \frac{e_3^2}{G}$$

$$= \frac{l^2}{b^2 (EA)_e} \left[1 + k_d + \frac{1}{2} k_b - \frac{2}{3} \right] - \frac{l^2 l^2}{b^2 l^2 (EA)_e} \frac{[1 + k_d + \frac{1}{2} k_b]^2}{[1 + 2k_a + k_d + \frac{1}{2} k_b]} \times [1 + 2k_a + k_d + \frac{1}{2} k_b]$$

$$= \frac{l^2}{b^2 (EA)_e} \left\{ \left[\frac{1}{3} + k_d + \frac{1}{2} k_b \right] - \frac{[1 + k_d + \frac{1}{2} k_b]^2}{[1 + 2k_a + k_d + \frac{1}{2} k_b]} \right\}$$

$$= \frac{l^2}{b^2 (EA)_e} \frac{\frac{1}{3}(1 + 2k_a) + (\frac{1}{3} + 1 + 2k_a + k_d + \frac{1}{2} k_b) - 1 - 2 \left(\frac{1}{3} + k_d + \frac{1}{2} k_b \right)}{1 + 2k_a + k_d + \frac{1}{2} k_b}$$

$$= \frac{l^2}{b^2 (EA)_e} \frac{\frac{2}{3} k_a - \frac{2}{3} + (k_d + \frac{1}{2} k_b)(2k_a - \frac{2}{3})}{1 + 2k_a + k_d + \frac{1}{2} k_b}$$

$$= \frac{2}{3} \frac{l^2}{b^2 (EA)_e} \frac{[(k_a - 1) + (3k_a - 1)(k_d + \frac{1}{2} k_b)]}{[1 + 2k_a + k_d + \frac{1}{2} k_b]}$$

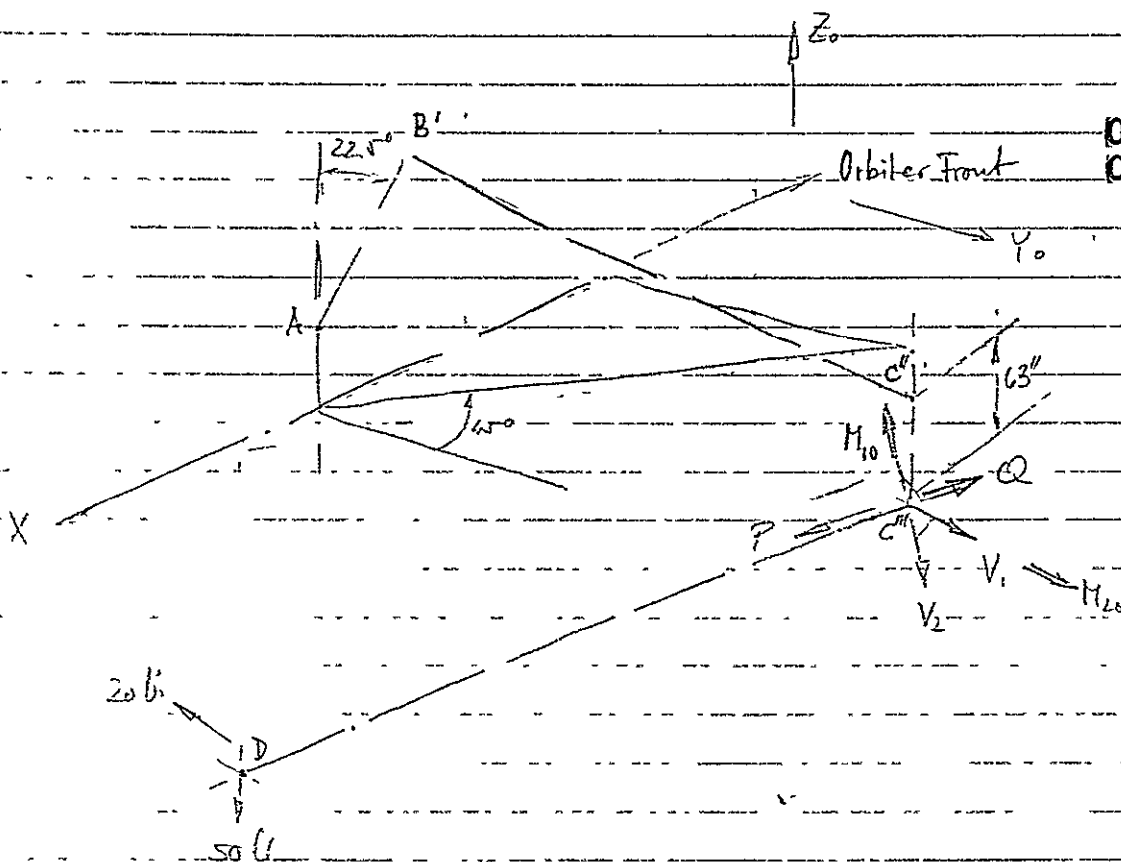
APPENDIX C

EXTERNAL FORCES ALONG LOWER AND UPPER ARMS

External Forces along Lower and Upper Arms.

(11) C-12-78

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unit vector in V₂ direction

$$(-\sin 8^{\circ}50' \sin 13^{\circ}33', \sin 8^{\circ}50' \cos 46^{\circ}52', -\cos 8^{\circ}50')$$

$$\bar{U}_2 = (-1158, 1009, -9881)$$

$$\text{in } V \text{ direction} = \frac{(\bar{U}_3 \times \bar{U}_2)}{|\bar{U}_3 \times \bar{U}_2|} = (8570, 7539, 0)$$

$$\bar{U}_1 = (\cos 46^{\circ}52', \sin 46^{\circ}52', 0)$$

$$\text{Thus, } V_{1e} = \bar{F} \cdot \bar{U}_1 = -20 \cdot \bar{F} \cdot \cos 46^{\circ}52' = -20 \cdot \bar{F} \cdot 0.6893 \quad \bar{F} = (-20 \cos 13^{\circ}33', -20 \sin 13^{\circ}33', -50)$$

$$V_{2e} = \bar{F} \cdot \bar{U}_2 = 1004 \cdot -0.9881$$

$$P_e = \bar{F} \cdot \bar{U}_3 = 77 = -20 \sin 13^{\circ}33'$$

$$\text{center of mass } C_e = -20 \left(\frac{11}{2} + 6 \right) \quad X = \frac{h}{L_e} = 584 \pm 2$$

$$M_{1e} = 0$$

$$M_{2e} = 0$$

5-12-72

at C^{III}

$$V_{10L} = -20$$

$$X_{10L} = 0$$

$$V_{20L} = 49.4$$

$$P_{0L} = 7.7$$

$$M_{10L} = V_{1L} \times 584.33 = -11,687 \text{ in lb}$$

$$M_{20L} = 49.4 \times 584.33 = 28,866 \text{ in lb}$$

$$Q_{0L} = -20 \left(\frac{b}{2} + 6 \right) = -20 \times 25.48 = -510$$

Transformation to upper arm

rotate up $8^{\circ}50'$

$$V_{10L} \rightarrow V_{10L}$$

$$V_{20L} \rightarrow V_{20L} \cos 8^{\circ}50' + P_{0L} \sin 8^{\circ}50'$$

$$P_{0L} \rightarrow -V_{20L} \sin 8^{\circ}50' + P_{0L} \cos 8^{\circ}50'$$

$$M_{10L} \rightarrow M_{10L} \cos 8^{\circ}50' + Q_{0L} \sin 8^{\circ}50'$$

$$M_{20L} \rightarrow M_{20L}$$

$$Q_{0L} \rightarrow -M_{10L} \sin 8^{\circ}50' + Q_{0L} \cos 8^{\circ}50'$$

rotate 3.93° about new M_{10}/V_{20} axis

$$V_{10L} \rightarrow V_{10L} \cos 3.93^\circ + (-V_{20L} \sin 8^\circ 50' - P_{0L} \sin 8^\circ 50') \sin 3.93^\circ$$

$$V_{20L} \rightarrow V_{20L} \cos 8^\circ 50' + P_{0L} \sin 8^\circ 50'$$

$$P_{0L} \rightarrow (-V_{20L} \sin 8^\circ 50' + P_{0L} \cos 8^\circ 50') \cos 3.93^\circ - V_{10L} \sin 3.93^\circ$$

$$M_{10L} \rightarrow M_{10L} \cos 3.93^\circ + Q_{0L} \sin 3.93^\circ$$

$$M_{20L} \rightarrow M_{20L} \cos 3.93^\circ - (-M_{10L} \sin 8^\circ 50' + Q_{0L} \cos 8^\circ 50') \sin 3.93^\circ$$

$$Q_{0L} \rightarrow M_{20L} \sin 3.93^\circ + (-M_{10L} \cos 8^\circ 50' + Q_{0L} \sin 8^\circ 50') \cos 3.93^\circ$$

translate up to C'' (.63 in. in. + $Z_{0,dis}$)

no change in V_1, V_2, P, M_{10}

$$P_{20} \rightarrow P_{20L} \cos 3.93^\circ + (M_{10L} \sin 8^\circ 50' - Q_{0L} \cos 8^\circ 50') \sin 3.93^\circ -$$

$$.63 [(P_{0L} \cos 8^\circ 50' - V_{20L} \sin 8^\circ 50') \cos 3.93^\circ - V_{10L} \sin 3.93^\circ]$$

$$Q_{0} \rightarrow M_{20L} \sin 3.93^\circ - (M_{10L} \cos 8^\circ 50' - Q_{0L} \sin 8^\circ 50') \cos 3.93^\circ -$$

$$.63 [(P_{0L} \sin 8^\circ 50' - V_{20L} \cos 8^\circ 50') \sin 3.93^\circ + V_{10L} \cos 3.93^\circ]$$

5-12-76

rotate up 22.5° about V_1, H_{20} axis

$$V_{10}'' = V_{10} \cos 39.3^\circ + (P_0 \cos 8^\circ 50' - V_{20} \sin 8^\circ 50') \sin 39.3^\circ$$

$$V_{20}'' = (V_{20} \cos 8^\circ 50' - P_0 \sin 8^\circ 50') \cos 22.5^\circ + [(P_0 \cos 8^\circ 50' - V_{20} \sin 8^\circ 50') \cos 39.3^\circ - V_{10} \sin 39.3^\circ]$$

$$P_0'' = -(V_{20} \cos 8^\circ 50' - P_0 \sin 8^\circ 50') \sin 22.5^\circ + [(P_0 \cos 8^\circ 50' - V_{20} \sin 8^\circ 50') \cos 39.3^\circ - V_{10} \sin 39.3^\circ]$$

$$H_{10}' = (H_{10} \cos 39.3^\circ + Q_0 \sin 39.3^\circ) \cos 22.5^\circ +$$

$$+ \sin 22.5^\circ \{ H_{20} \sin 39.3^\circ - (H_{10} \sin 8^\circ 50' - Q_0 \cos 8^\circ 50') \cos 39.3^\circ -$$

$$- 63 [(P_0 \cos 8^\circ 50' - V_{20} \sin 8^\circ 50') \sin 39.3^\circ - V_{10} \cos 39.3^\circ]$$

$$H_{20}' = H_{20} \cos 39.3^\circ + (H_{10} \sin 8^\circ 50' - Q_0 \cos 8^\circ 50') \sin 39.3^\circ -$$

$$- 63 [(P_0 \cos 8^\circ 50' - V_{20} \sin 8^\circ 50') \cos 39.3^\circ - V_{10} \sin 39.3^\circ]$$

$$Q_0'' = -(H_{10} \cos 39.3^\circ + Q_0 \sin 39.3^\circ) \sin 22.5^\circ +$$

$$+ \{ H_{20} \sin 39.3^\circ - (H_{10} \sin 8^\circ 50' - Q_0 \cos 8^\circ 50') \cos 39.3^\circ - 63 [(P_0 \cos 8^\circ 50' - V_{20} \sin 8^\circ 50') \sin 39.3^\circ + V_{10} \cos 39.3^\circ] \}$$

normalization for upper arm

$$\begin{array}{l} \text{at } C'' \\ \left\{ \begin{array}{l} V_{1u} = V_{10}'' \\ V_{2u} = -V_{20}'' \\ P_u = -P_0'' \\ H_{1u} = -H_{10}'' \\ H_{2u} = P_{20}'' \\ Q_u = -Q_0'' \end{array} \right. \end{array} \quad \begin{array}{l} \text{at } B' \\ \left\{ \begin{array}{l} V_{10u} = V_{10}'' \\ V_{20u} = -V_{20}'' \\ P_{0u} = -P_0'' \\ H_{10u} = -H_{10}'' = V_{10}'' l_u \\ H_{20u} = H_{20}'' = V_{20}'' l_u \\ Q_{0u} = -Q_0'' \end{array} \right. \end{array}$$

APPENDIX D

COMPLIANCE (CASTIGLIANO)

Compliance use Castigliano (without shear!)

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- define external loads

- define moments along lower and upper arm (transformation at elbow) in terms of V_1, V_2, P

- determine strain energy by integrating along both upper and lower arm

- determine deflection

note: p (17) $V_{1e} = -20$ $x = 584.33$

$$V_{2e} = 49.4$$

$$P_e = 77$$

$$M_{1e}' = 0$$

$$M_{2e} = 0$$

$$Q_e = V_{1e} \times 2548 = -510$$

note: these loads are with reference to \hat{e} of panel not neutral axis

for neutral axis

$$H_1(x=584.33) = P_e e_1 = 77 e_1$$

$$Q(x=584.33) = -510 - V_2 e_3 = -(510 + 49.4 e_3)$$

at root of lower arm (elbow)

forces same

$$\text{moment: } M'_{10} = V_{1c} \times \ell_c = -20 \times 584.33 = -11,687$$

$$M_{20} = V_{2c} \times \ell_c = 494 \times 584.33 = 288,866$$

$$Q_0 = Q_c = -510$$

for integration

$$M_{10} = P_{\ell} \cdot e_1 + M'_{1c} = P_{\ell} e_1 + V_{1c} \ell_c$$

moments along neutral axis (x origin at elbow)

$$M_1(x) = M_{10} - V_{1c} x = P_{\ell} e_1 + V_{1c} (\ell_c - x)$$

$$M_2(x) = M_{20} - V_{2c} x = V_{2c} (\ell_c - x)$$

$$Q(x) = Q_c = Q_e = V_{1c} \times 2548 - V_{2c} e_3$$

$$U_{\ell} = (SE)_{\text{lower arm}} = \int_0^{\ell_c} \left[\frac{M_1(x)^2}{2EI_1} + \frac{M_2(x)^2}{2EI_2} + \frac{Q(x)^2}{2GJ} \right] dx$$

$$\frac{\partial U_{\ell}}{\partial V_{1c}} = \int_0^{\ell_c} \left[\frac{M_1(x)}{EI_1} \frac{\partial M_1}{\partial V_{1c}} + \frac{M_2(x)}{EI_2} \frac{\partial M_2}{\partial V_{1c}} + \frac{Q(x)}{GJ} \frac{\partial Q}{\partial V_{1c}} \right] dx$$

$$= \int_0^{\ell_c} \left[\frac{(P_{\ell} e_1 + V_{1c} (\ell_c - x)) (\ell_c - x)}{EI_1} + 0 + \frac{(V_{1c} 2548 - V_{2c} e_3) 2548}{GJ} \right] dx$$

$$= V_{1c} \left[\frac{1}{EI_1} \frac{\ell_c^3}{3} + \frac{2548^2 \ell_c}{GJ} \right] - V_{2c} \left[\frac{e_3 \times 2548 \ell_c}{GJ} + P_{\ell} \frac{e_1 \ell_c}{EI_1} \right]$$

$$\frac{\partial U}{\partial V_{2e}} = \int_0^{l_e} \left[0 + \frac{V_{2e}(l_e - x)^2}{EI_2} - \frac{(V_{1e} 2548 - V_{2e} e_3) e_3}{GJ} \right] dx$$

$$= V_{1e} \left(-\frac{2548 e_3 l_e}{GJ} \right) + V_{2e} \left(\frac{l_e^3}{3EI_2} + \frac{e_3^2 l_e}{GJ} \right) + P_e = 0$$

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$$\frac{\partial U}{\partial P_e} = \int_0^{l_e} \frac{P_e e_1 + V_{1e}(l_e - x)}{EI_1} e_1 dx$$

$$= V_{1e} \left(\frac{e_1 l_e^2}{2EI_1} \right) + V_{2e} \cdot 0 + P_e \left(\frac{e_1 l_e}{EI_1} \right)$$

now transform \bar{T}_{to} into $\bar{T}_u (x=552)$ see γ (18) to (20)

$$\begin{bmatrix} V_{1u} \\ V_{2u} \\ P_u \\ H'_{1u} \\ P_{2u} \\ Q_u \end{bmatrix} = \begin{bmatrix} T_{11} & T_{12} & T_{13} & T_{14}=0 & T_{15}=0 & T_{16}=0 \\ T_{21} & T_{22} & & 0 & 0 & 0 \\ T_{31} & & T_{33} & 0 & 0 & 0 \\ T_{41} & & & T_{44} & & \\ T_{51} & & & & T_{55} & \\ T_{61} & & & & & T_{66} \end{bmatrix} \begin{bmatrix} V_{1e} \\ V_{2e} \\ P_e \\ H'_{1oe} \\ M_{2oe} \\ Q_{oe} \end{bmatrix}$$

5-17-78

$$T_{11} = \cos 3.93 \quad 99765$$

$$T_{12} = -\sin 3.93 \sin 8^{50} \quad -010525$$

$$T_{13} = \sin 3.93 \cos 8^{50} \quad 067725$$

$$T_{14} \text{ to } T_{16} = 0$$

$$T_{21} = \sin 3.93 \sin 22.5 \quad -026228$$

$$T_{22} = -\cos 8^{50} \cos 22.5 + \cos 3.93 \sin 8^{50} \sin 22.5 \quad -85429$$

$$T_{23} = -\sin 8^{50} \cos 22.5 - \cos 3.93 \cos 8^{50} \sin 22.5 \quad -51913$$

$$T_{24} \text{ to } T_{26} = 0$$

$$T_{31} = \sin 3.93 \cos 22.5 \quad 0633205$$

$$T_{32} = \cos 8^{50} \sin 22.5 + \cos 3.93 \sin 8^{50} \cos 22.5 \quad 57968$$

$$T_{33} = \sin 8^{50} \sin 22.5 - \cos 3.93 \cos 8^{50} \cos 22.5 \quad -85201$$

$$T_{34} \text{ to } T_{36} = 0$$

$$T_{41}/T_{41}' = 63 \cos 3.93 \sin 22.5 \quad 24.052 \quad / \quad -140.37$$

$$T_{42}/T_{42}' = -63 \sin 3.93 \sin 8^{50} \sin 22.5 \quad -2537 \quad / \quad -141.75$$

$$T_{43} = 63 \sin 3.93 \cos 8^{50} \sin 22.5 \quad 16328$$

$$T_{44} = -\cos 3.93 (\cos 22.5 - \sin 8^{50} \sin 22.5) \quad -86308$$

$$T_{45} = \sin 3.93 \sin 22.5 \quad -026228$$

$$T_{46} = -\sin 3.93 \cos 22.5 + \cos 3.93 \cos 8^{50} \sin 22.5 \quad 31393$$

5-17-78

cm 6-2-78

$$T_{51}/I_5' = 63 \sin 3.93$$

$$4.3179 / 8.4010874$$

$$T_{52}/I_5' = 63 \cos 3.93 \sin 8.00$$

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$$9.6516 / 560.3555$$

$$T_{53} = -63 \cos 3.93 \cos 8.00$$

$$-62.106$$

$$T_{54} = \sin 3.93 \sin 8.00$$

$$0.10525$$

$$T_{55} = \cos 3.93$$

$$99.765$$

$$T_{56} = -\sin 3.93 \cos 8.00$$

$$-0.67765$$

$$T_{61}/I_6' = 63 \cos 3.93 \cos 22.5$$

$$58.0675 / 324.40341$$

$$T_{62}/I_6' = -63 \sin 3.93 \sin 8.00 \cos 22.5$$

$$-61.258 / 35.566-3$$

$$T_{63} = 63 \sin 3.93 \cos 8.00 \cos 22.5$$

$$3.9419$$

$$T_{64} = \cos 3.93 (\sin 22.5 + \sin 8.00 \cos 22.5)$$

$$52.332$$

$$T_{65} = -\sin 3.93 \cos 22.5$$

$$-0.63326$$

$$T_{66} = \sin 3.93 \sin 22.5 - \cos 3.93 \cos 8.00 \cos 22.5$$

$$-88.454$$

note because the moments are functions of V_{1c}, V_{2c}, V_c

the matrix can be reduced to a 6x6 type

for forces at shoulder (root of upper arm see p. 20)

reduce matrix $M_{10} e = V_{1e} l_e$

$$M_{20} e = V_{2e} l_e$$

$$Q_{0e} = V_{1e} 2548$$

Thus

$$\begin{bmatrix} V_{1e} \\ V_{2e} \\ P_e \\ M_{1e}' \\ M_{2e}' \\ Q_e \end{bmatrix} = \begin{bmatrix} T_{11} & T_{12} & T_{13} \\ T_{21} & T_{22} & T_{23} \\ T_{31} & T_{32} & T_{33} \\ \left(\frac{T_{41}'}{T_{41} + T_{44} l_e + T_{46} 2548} \right) & \left(\frac{T_{42}'}{T_{42} + T_{45} l_e} \right) & T_{43} \\ \left(\frac{T_{51}'}{T_{51} + T_{54} l_e + T_{56} 2548} \right) & \left(\frac{T_{52}'}{T_{52} + T_{55} l_e} \right) & T_{53} \\ \left(\frac{T_{61}'}{T_{61} + T_{64} l_e + T_{66} 2548} \right) & \left(\frac{T_{62}'}{T_{62} + T_{65} l_e} \right) & T_{63} \end{bmatrix} \begin{bmatrix} V_{1e} \\ V_{2e} \\ P_e \end{bmatrix}$$

moment distribution in upper arm

$$M_{1u}(x) = M_{1e}' + P_e e_1 + V_{1e} (l_u - x)$$

$$M_{2u}(x) = M_{2e}' + V_{2e} (l_u - x)$$

$$Q_u(x) = Q_e - V_{2e} e_3$$

$$U_u = \int_0^{l_u} \left[\frac{M_{1u}^2}{2EI_1} + \frac{M_{2u}^2}{2EI_2} + \frac{Q_u^2}{2GJ} \right] dx$$

$$\lim_{\Delta x \rightarrow 0} \frac{\partial U_u}{\partial V_u} = \int_0^l \left\{ \frac{1}{EI_1} [M_{1u}' + P_u e_1 + V_u(l-x)] [T_{41} + T_{44}l + T_{46} + 25.48 + T_{31}e_1 + T_{11}(l-x)] \right. \\ \left. + \frac{1}{EI_2} [M_{2u}' + V_{2u}(l-x)] [T_{51} + T_{54}l + T_{56} + 25.48 + T_{21}(l-x)] \right. \\ \left. + \frac{1}{GJ} [Q_u - V_{2u}e_3] [T_{61} + T_{64}l + T_{66} + 25.48 + T_{21}e_3] \right\} dx$$

$$= \frac{1}{EI_1} \left\{ (M_{1u}' + P_u e_1) \overbrace{(-T_{41} + T_{44}l + T_{46} + 25.48 + T_{31}e_1)}^{T_{41}'} l_u \right. \\ \left. + [(M_{1u}' + P_u e) T_{11} + V_{1u} \left(\frac{1}{EI_1} \right)] \frac{l_u^2}{2} + V_{1u} T_{11} \frac{l_u^3}{3} \right\}$$

$$+ \frac{1}{EI_2} \left\{ M_{2u} (T_{51} + T_{54}l + T_{56} + 25.48) l_u + \right. \\ \left. [M_{2u} T_{21} + V_{2u} \left(\frac{1}{EI_2} \right)] \frac{l_u^2}{2} + V_{2u} T_{21} \frac{l_u^3}{3} \right\}$$

$$+ \frac{l_u}{GJ} [Q_u - V_{2u}e_3] \left[\frac{T_{61} + T_{64}l + T_{66} + 25.48}{T_{61}'} - T_{21}e_3 \right] =$$

$$= V_{1E} \left\{ \frac{1}{EI_1} [(T_{41}' + T_{31}e_1)^2 l_u + 2(T_{41}' - T_{31}e_1) T_{11} \frac{l_u^2}{2} + T_{11}^2 \frac{l_u^3}{3}] \right.$$

$$+ \frac{1}{EI_2} [T_{51}'^2 l_u + 2T_{51}' T_{21} \frac{l_u^2}{2} + T_{21}^2 \frac{l_u^3}{3}]$$

$$+ \frac{l_u}{GJ} (T_{61}' - T_{21}e_3)^2 \left. \right\}$$

$$+ V_{2E} \left\{ \frac{1}{EI_2} [(T_{44}' - T_{22}e_1)(T_{44}' + T_{22}e_1) l_u + [(T_{44}' - T_{22}e_1) T_{11} + T_{11}(T_{44}' - T_{22}e_1)] \frac{l_u^2}{2} + T_{11} T_{11} \frac{l_u^3}{3} \right\}$$

$$+ \frac{1}{EI_2} \left[T_{52}' T_{51}' l_u + (T_{52}' T_{21} + T_{22} T_{51}') \frac{l_u^2}{2} + T_{22} T_{21} \frac{l_u^3}{3} \right]$$

$$+ \frac{l_u}{GJ} [(T_{62}' - T_{22} e_3)(T_{61}' - T_{21} e_3)] \Bigg\}$$

$$+ P_c \left\{ \frac{1}{EI_1} \left[(T_{43} + T_{33} e_1)(T_{41}' + T_{31} e_1) l_u + [(T_{43} + T_{33} e_1) T_{41} + T_{13} (T_{41}' + T_{31} e_1)] \frac{l_u^2}{2} + T_{13} T_{41} \right] \right.$$

$$+ \frac{1}{EI_2} \left[T_{53} T_{51}' l_u + (T_{53} T_{21} + T_{23} T_{51}') \frac{l_u^2}{2} + T_{23} T_{21} \frac{l_u^3}{3} \right]$$

$$+ \frac{l_u}{GJ} (T_{63} - T_{23} e_3)(T_{61}' - T_{21} e_3) \Bigg\}$$

$$\frac{\partial U_u}{\partial V_{2u}} = - \int_0^{l_u} \left\{ \frac{1}{EI_1} (M_{1u}' + P_u e_1 + V_{1u}' l_u - x) (T_{4u}' + T_{3u} e_1 + T_{12} (l_u - x)) \right.$$

$$- \frac{1}{EI_2} (M_{2u} + V_{2u} (l_u - x)) (T_{52}' + T_{22} (l_u - x))$$

$$+ \frac{1}{GJ} (Q_u - V_{2u} e_3) (T_{62}' - T_{22} e_3) \Bigg\} dx$$

$$= - \frac{1}{EI_1} \left\{ (M_{1u}' + P_u e_1)(T_{4u}' + T_{3u} e_1) l_u + [M_{1u}' + P_u e_1] T_{12} l_u + V_{1u} (T_{41}' + T_{31} e_1) \frac{l_u^2}{2} + V_{1u} T_{12} \frac{l_u^3}{3} \right.$$

$$+ \frac{1}{EI_2} \left\{ (M_{2u} T_{52}' l_u + (M_{2u} T_{22} + V_{2u} T_{52}') \frac{l_u^2}{2} + V_{2u} T_{22} \frac{l_u^3}{3} \right\}$$

$$+ \frac{1}{GJ} (Q_u - V_{2u} e_3) (T_{62}' - T_{22} e_3) l_u$$

$$= V_{1L} \left\{ \frac{1}{EI_1} \left[(T_{41}' + T_{31} e_1)(T_{42}' + T_{32} e_1) l_u + \left\{ (T_{41}' + T_{31} e_1) T_{12} + T_{11} (T_{42}' + T_{32} e_1) \right\} \frac{l_u^2}{2} + T_{11} T_{12} \frac{l_u^3}{3} \right] \right.$$

$$+ \frac{1}{EI_2} \left[T_{51}' T_{52}' l_u + (T_{51}' T_{22} + T_{21} T_{52}') \frac{l_u^2}{2} + T_{21} T_{22} \frac{l_u^3}{3} \right] \left. \right.$$

$$+ \frac{l_u}{GJ} (T_{61}' - T_{21} e_3)(T_{62}' - T_{22} e_3) \left. \right\}$$

$$+ V_{2L} \left\{ \frac{1}{EI_1} \left[(T_{42}' + T_{32} e_1)^2 l_u + 2(T_{42}' + T_{32} e_1) T_{12} \frac{l_u^2}{2} + T_{12}^2 \frac{l_u^3}{3} \right] \right.$$

$$+ \frac{1}{EI_2} \left[T_{51}'^2 l_u + 2 T_{51}' T_{22} \frac{l_u^2}{2} + T_{22}^2 \frac{l_u^3}{3} \right]$$

$$+ \frac{l_u}{GJ} (T_{62}' - T_{22} e_3)^2 \left. \right\}$$

$$+ V_{3L} \left\{ \frac{1}{EI_1} \left[(T_{43}' + T_{33} e_1)(T_{42}' + T_{32} e_1) l_u + \left\{ (T_{43}' + T_{33} e_1) T_{12} + T_{13} (T_{42}' + T_{32} e_1) \right\} \frac{l_u^2}{2} + T_{12} T_{13} \frac{l_u^3}{3} \right] \right.$$

$$+ \frac{1}{EI_2} \left[T_{53} T_{52}' l_u + (T_{53} T_{22} + T_{22} T_{52}') \frac{l_u^2}{2} + T_{22} T_{22} \frac{l_u^3}{3} \right]$$

$$+ \frac{l_u}{GJ} (T_{62}' - T_{22} e_2)(T_{62}' - T_{22} e_2) \left. \right\}$$

$$\begin{aligned}
 \frac{\partial U_u}{\partial P_e} &= - \int_0^L \left\{ \frac{1}{EI_1} (M_{1u}' + P_u e_1 + V_{1u} (l_u - x)) (T_{43} + T_{32} e_1 + T_{12} (l_u - x)) \right. \\
 &\quad + \frac{1}{EI_2} (M_{2u} + V_{2u} (l_u - x)) (T_{53} + T_{23} (l_u - x)) \\
 &\quad \left. + \frac{1}{GJ} (Q_u - V_{2u} e_3) (T_{63} - T_{22} e_3) \right\} dx \\
 &= - \frac{1}{EI_1} \left\{ (M_{1u}' + P_u e_1) (T_{43} + T_{32} e_1) l_u + [(M_{1u}' + P_u e_1) T_{12} + V_{1u} (T_{43} + T_{32} e_1)] \frac{l_u^2}{2} + V_{1u} T_{12} \frac{l_u^3}{3} \right\} \\
 &\quad + \frac{1}{EI_2} \left\{ M_{2u} T_{53} l_u + (M_{2u} T_{23} + V_{2u} T_{53}) \frac{l_u^2}{2} + V_{2u} T_{23} \frac{l_u^3}{3} \right\} \\
 &\quad + \frac{l_u}{GJ} (Q_u - V_{2u} e_3) (T_{63} - T_{22} e_3) \\
 &= V_{1u} \left\{ \frac{1}{EI_1} \left[(T_{41}' + T_{31} e_1) (T_{12} + T_{32} e_1) l_u + [(T_{41}' + T_{31} e_1) T_{12} + T_{11} (T_{43} + T_{32} e_1)] \frac{l_u^2}{2} + T_{11} T_{12} \frac{l_u^3}{3} \right] \right. \\
 &\quad + \frac{1}{EI_2} \left[T_{51}' T_{53} l_u + (T_{51}' T_{23} + T_{21} T_{53}) \frac{l_u^2}{2} + T_{21} T_{23} \frac{l_u^3}{3} \right] \\
 &\quad \left. + \frac{l_u}{GJ} (T_{61}' - T_{21} e_3) (T_{63} - T_{22} e_3) \right\} \\
 &\quad + V_{2u} \left\{ \frac{1}{EI_1} \left[(T_{42} - T_{32} e_1) (T_{12} + T_{32} e_1) l_u + [(T_{42} - T_{32} e_1) T_{12} + T_{12} (T_{43} + T_{32} e_1)] \frac{l_u^2}{2} + T_{12} T_{12} \frac{l_u^3}{3} \right] \right. \\
 &\quad + \frac{1}{EI_2} \left[T_{52}' T_{53} l_u + (T_{52}' T_{23} + T_{22} T_{53}) \frac{l_u^2}{2} + T_{22} T_{23} \frac{l_u^3}{3} \right] \\
 &\quad \left. + \frac{l_u}{GJ} (T_{62} - T_{22} e_3) (T_{63} - T_{22} e_3) \right\} \\
 &\quad + P_e \left\{ \frac{1}{EI_1} \left[(T_{43} + T_{32} e_1) l_u + 2 (T_{43} + T_{32} e_1) T_{12} \frac{l_u^2}{2} + T_{12}^2 \frac{l_u^3}{3} \right] \right. \\
 &\quad + \frac{1}{EI_2} \left[T_{53} l_u + 2 T_{53} T_{23} \frac{l_u^2}{2} + T_{23}^2 \frac{l_u^3}{3} \right] \\
 &\quad \left. + \frac{l_u}{GJ} (T_{63} - T_{23} e_3) \right\}
 \end{aligned}$$

APPENDIX E

VARIATION OF ARM POSITION

Variation of Arm Position

calculate margin when forces remain 50 lb in Z direction
± 20 lb perpendicular to lower arm pan

	position II	III	IV
angles	22.5 remains		
3.93 change to	-30	-70	-102.5
8% change to	6°	2.7°	0

distance V_f	580.32	628	565	715
Force \overline{F}_f	V_1	±20	±20	±20
	V_2	497	499	50
	P	52	24	0
	Q_1	±510	±510	±510

\overline{F}_c'''	V_1	±20	±20	±20
	V_2	497	499	50
	P	52	24	0
	H_{10}'	±12560	±11300	±14300
	H_{20}	31,230	28,220	35,750
	Q	±510	±510	±510

		q_1	q_2	q_1	q_2	q_1	q_2
\overline{F}_c''	V_1	-1731	1733	-6.88	6.80	4.33	-1.53
	V_2	-42.33	-45.99	-32.97	-18.51	-38.72	-53.61
	P	28.38	9.50	36.47	12.11	37.17	1.09
	H_{10}'	14,769	-2817	12,973	-2355	10184	10,529
	H_{20}	28,680	26,015	10,256	15,116	-7006	-8470
	Q	8,709	36,949	22,706	12,313	33,771	30,121

Transformation Matrix $[T_{ij}]$

Position	I	II	III	IV
β	393°	-30°	-70°	-102.5°
ϵ	8.76°	6°	27°	0°
T_{11}	.99765	.86603	.34202	-.21644
T_{12}	-.010525	.052264	.044266	0
T_{13}	.067725	-.49726	-.93865	-.97520
T_{14}	.026228	-.19134	-.35960	-.37361
T_{22}	-.85429	-.88418	-.91669	-.92388
T_{23}	-.51913	-.42617	-.17426	.082828
T_{21}	.0632205	.46194	-.86816	-.90198
T_{32}	.51868	.46422	.39714	.38268
T_{33}	-.85201	-.75772	-.29761	.19996
T_{11}'	24.052	-472.27	20.879	439.661
T_{12}'	-.2537	-15580	1.2600	121.622
T_{13}'	1.6328	-11.928	-22.630	-23.532
T_{14}'	-.86203	-.76546	-.30982	.19996
T_{22}'	-.026228	.19134	.35960	.37361
T_{23}'	.31551	.79156	.99890	.81915
T_{31}'	4.3179	8.742	-.315	-51.652
T_{32}'	9.6555	57.106	5.7030	50.9570
T_{33}'	-62.106	-.54.261	-21.523	+13.636
T_{34}'	-.010525	-.052264	-.044266	0
T_{41}'	.99765	.86603	.34202	-.21644
T_{42}'	-.067725	.49726	.93865	.97630
T_{61}/T_{51}'	.580675/341.321	50.4065	.285	.968
T_{21}'	-.61258	-37.47	3.0420	.293
T_{11}	3.9412	-.28.943	-.54.634	-.56.825
T_{12}	.52551	.4505	.14577	-.052820
T_{13}	-.0632205	.46194	.86816	.90198
T_{14}	-.82454	-.92709	-.67524	-.175

57
5-2'

	II	I	IV
$\bar{F} (x_u = 52.34)$	V_1	-17.31 17.33	-6.88 6.80 4.23 -4.35
	V_2	-42.33 -49.99	-38.97 -48.97 -38.72 -53.67
	P	28.38 9.30	36.47 12.11 37.17 1.09
ORIGINAL PAGE IS OF POOR QUALITY	M_{10}'	14.172 -2219	12.736 -2160 10.333 16.320
	M_{10}	26.620 14.290	9.512 13.471 -8.342 -10.322
	Q_1	8.709 36.949	22.796 18.313 33.771 30.721

$\bar{F} (x_u = 34.5)$	V_1	-17.31 17.33	-6.88 6.80 4.33 -4.33
	V_2	-42.33 -49.99	-38.97 -48.97 -38.72 -53.67
	P	28.38 9.30	36.47 12.11 37.17 1.09
	M_{10}'	6.330 5.631	9.619 9.20 12.295 14.418
	M_{10}	74.44 16.45	-81.42 -2713 -25.882 -34.634
	Q_1	8.709 36.949	22.796 18.313 33.771 30.721

$\bar{F} (x_L = 34.5)$	V_1	20	20 20
	V_2	49.7	49.9 50
	P	5.2	2.4 0
	M_{10}'	11.820	10.610 13.610
	M_{10}	29.515	26.498 34.025
	Q_1	510	510 510

Note second number is for second quadrant (20 lb force reversed)

APPENDIX F

FORCES IN TRUSS MEMBERS (NUMERICAL) AND MARGINS OF SAFETY

Forces in Truss Members and Margins of Safety (Vertical Loader)

Applied load 20 lb in X-Y plane of Orbiter
50 lb in -Z direction

Quadrant 1 $V_1 = -20$
2 $V_1 = +20$
3 $V_1 = +20$ 50 lb reversed
4 $V_1 = -20$ 50 lb reversed

Euler buckling of members $\frac{\pi^2 EI_d}{L^2}$ where $L = l, a, b, d$

	Aluminum	CRS	C/epoxy
Longeron 1 & 2	5,232	8,864	8,268
Main Scissor (2L)	1,475 ¹⁾ 1,630 ²⁾	2,216	2,067
A-Frame	3,222	8,614	5,092
Cross brace, single	4,102	6,949	6,482
Diagonal brace	2,300	3,895	3,635

¹⁾ 625 ID

²⁾ full cross section

Yield Limits

	Aluminum (35 ksi)	CRS (58 ksi)
Main Scissor	24,050 ¹⁾ 34,800	17,215
Other Members	19,300	17,215

¹⁾ 625 ID

²⁾ full cross section

Bearing Loads in Aluminum joints

pin dia = 1875 bearing width = 25 $\sigma_{b,all} = 56 \text{ ksi}$

bearing load max = 2,625 lb

$$\text{Margin} = \frac{P_{\text{rel}}}{3P} - 1$$

Q1 quadrant

(58)
5-24-7

member force

position

I

II

III

IV

P_{Au}

-535.80 1.00

495.7 1.17

1341.9 -1.20

2004.6 -1.46

P_{Bu}

489.74 1.19

-535.6 1.00

-1357.7 -1.21

-1994.7 -1.46

P_{du}

-544.14 .41

666.9 .15

1649.8 -1.54

2418.7 -1.68

P_{lu}

407.39 2.36

-499.3 1.74

-1235.2 .11

-1810.8 -1.24

P_{Al}

-53.27

-53.27

-53.27

-53.3

P_{El}

7.13

7.13

7.13

7.13

P_{Ec}

-101.73

-102.13

-102.40

-102.53

P_{Lc}

76.16

76.46

76.66

76.76

$\lambda_u = 34.3$

P_1

229.0

813.5

1155.3

1211.7

P_2

192.4

-452.9

-614.1

-529.4

P_3

54.52

-332.2

-504.7

-654.2

$\lambda_u = 572.35$

P_1

551.32

1551.4

1690.2

1679.0

P_2

-113.67

-739.3

-985.4

-1099.6

P_3

-419.9

-763.7

-668.3

-542.2

$\lambda_c = 34.3$

P_1

368.62

381.0

335.0

448.2

P_2

-938.14

-998.6

-889.4

-1162.4

P_3

577.22

622.9

556.8

714.2

1st panel

P_{E1}

492.4

-70.7

61.6

-391.7

P_{E2}

-168.3

-10.8

479.6

1074.0

P_{E3}

90.7

-300.9

-492.3

-662.0

2nd panel

P_{E1}

131.7

371.4

-1032.1

-1295.1 -1.13

P_{E2}

192.4

-452.9

-614.1

-529.4

P_{E3}

18.4

-363.5

-517.1

-646.4

15th panel

P_{E1}

1272.8 .37

1109.3 .57

596.5 (1.92)

75.6

P_{E2}

-474.4

-297.2

108.3

503.8

P_{E3}

-383.7

-775.0 .737

-655.9 .25

-550.0

16th panel

P_{E1}

912.0

667.2

-497.2

-1527.6

P_{E2}

-113.7

-735.3

-925.4

-1099.6

P_{E3}

-455.5

712.4

-680.7

-531.1

91

(50)

5-24-78

		I	II	III	IV
1st - 1st	P_{e1}	503.5	516.4	470.8	584.1
1st panel	P_{e2}	-1005.6	-1066.3	-957.3	-1230.4
	P_s	613.4	659.1	593.0	750.4
2nd panel	P_{e1}	436.1	448.7	402.9	516.2
	P_{e2}	-938.1	-998.6	-889.4	-1162.4
	P_s	(541.0) \times $-.09$	586.7	520.6	(678.0) $-.27$

loads producing min. margin are circled

* 004 /r full com. section

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margin

20 lb force removed q_2

58.9

member	force	I	II	III	IV
P_{Au}		319.0 2.37	2207.8 -.81	1092.2 -.017	1814.1 -.41
P_{Bu}		-273.0 2.93	-2167.8 -.50	-1076.5 -.002	-1824.0 -.41
P_{du}		471.4 243.86 <u>2636.5</u>	-71 fail	13489 -.43	<u>2224.9</u> -.66 near fail.
P_{bu}		-308.0 3.44	-1988.9 -.31	-1010.0 .35	-1665.7 -.18
P_{Al}		53.3	53.3	53.3	53.3
P_{Bl}		-7.1	-7.1	-7.1	-7.1
P_{dl}		-30.2	-30.6	-30.9	-31.0
P_{ll}		22.6	22.9	23.1	23.2

$X_u = 24.5$

P_1	423.1	1956.0	700.8	864.9
P_2	-396.3	-1650.6	-602.4	-207.2
P_3	-6.4	-295.5	-48.3	-756.6

$X_u = 552-16.5$

P_1	736.4	2331.4	1189.3	1640.3
P_2	-1215.3	-2437.5	-1290.6	-779.7
P_3	499.3	115.9	113.3	-859.5

$X_c = 36.5$

P_1	969.5	428.4	-939.2	1209.8
P_2	-384.6	-1046.0	-380.0	-495.6
P_3	-577.2	622.9	-36.8	-714.2

margin

I

II

92

III

IV

59a

5-20-71

upper arm	P_{e1}	-122.4	-1566.1	-1087.6	<u>-2526.2</u>	-0.31
1 st panel	P_{e2}	-123.6	110.5	253.8	1538.7	.091
	P_s	-42.5	264.1	-60.6	-748.8	
2 nd panel	P_{e1}	150.4	194.9	-123.4	-781.0	
	P_{e2}	-396.3	-1650.6	-640.4	-207.2	
	P_s	29.7	326.9	-36.0	764.4	
1 st panel	P_{e1}	190.9	-1190.7	-599.1	-1851.4	
	P_{e2}	-942.6	-676.4	-396.4	966.2	
	P_s	463.2	84.5	101.0	<u>-851.7</u>	-0.42
						-36
16 th panel	P_{s1}	263.7	570.3	235.1	-105.6	-19
	P_{e1}	<u>-1215.3</u>	<u>-2437.5</u>	<u>-1290.6</u>	779.7	
	P_s	535.4	167.3	125.6	-867.3	
		1.26	.13	1.14		
lower arm	P_{e1}	1009.5	428.3	999.1	1250.9	
1 st panel	P_{e2}	-404.6	-1075.9	-350.1	-516.2	
	P_s	<u>-613.5</u>	<u>586.0</u>	<u>-553.1</u>	-750.5	
		-120	-114	-17		
		.12	.074	.16		
2 nd panel	P_{e1}	982.5	458.3	969.1	1230.4	
	P_{e2}	-384.6	-1016.0	-380.0	-495.6	
	P_s	<u>-540.9</u>	<u>659.2</u>	-520.5	-677.9	
		-09	.254			
		.27	.176			
			.045			

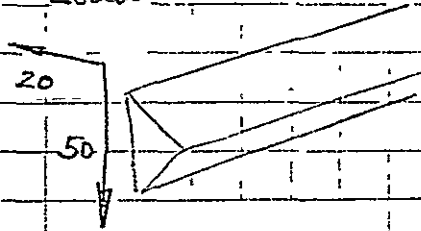
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margin with full Al sensor in black

margin for clep tubes 1115/815

Normalization of Load Limits

Code of Load



50 lb in -Z direction / 20 lb in X-Y plane forward

q_1 as given 50/20
 q_2 50/-20
 q_3 -50/-20
 q_4 -50/20

Arm Position	I	II	III	IV
Vertical Ladder				
Critical Member	S	D	D	D
Critical panel	lower No. 2	upper arm	upper arm	upper arm
Loading quadrant	q_2	q_4	q_3	q_3
Load Capacity with S.F.=3 % normalized load				
At Base	100%	23%	46%	31%

C/E_{oxy}
127 1/2
40%
65%
44%

Horizontal Ladder, C/E_{oxy}

Loading Quadrant q_2

Load Capacity with S.F.=3 105%
 % normalized load

APPENDIX G

COMPLIANCE MATRICES (NUMERICAL)

Compliances and Their Contributors

Configuration: Vertical Ladder, Position I Material: Aluminum

$$C_{ij} = \frac{10^6}{EI_1} \{ K_{11ij} + K_{u1ij} \} + \frac{10^6}{EI_2} \{ K_{22ij} + K_{u2ij} \} + \frac{10^6}{GJ} \{ K_{\theta\theta ij} + K_{u\theta ij} \}$$

$$l_c = 584.33 \quad e_1 = 9.027 \quad \frac{10^6}{EI_1} = 5263 \times 10^{-3} \quad \frac{10^6}{EI_2} = 2386 \times 10^{-3} \quad \frac{10^6}{GJ} = 3.7733 \times 10^{-3}$$

$$l_u = 552 \quad e_3 = 10.884 \quad \frac{10^6}{EI_1} \quad \frac{10^6}{EI_2} \quad \frac{10^6}{GJ}$$

i, j	C_{ij}	$K_{\theta 1}$	K_{u1}	$\frac{10^6}{EI_1} \{ K_{\theta 1} + K_{u1} \}$	$K_{\theta 2}$	K_{u2}	$\frac{10^6}{EI_2} \{ K_{\theta 2} + K_{u2} \}$	$K_{\theta \theta}$	$K_{u\theta}$	$\frac{10^6}{GJ} \{ K_{\theta \theta} + K_{u\theta} \}$
11	2.973	66.505	35.231	53.544×10^{-3}	0	150.62	0.3594×10^{-3}	3.794	64.200	243.677×10^{-3}
12	-0.1935	0	-2.0284	-7.093×10^{-3}	0	2.8337	6.761×10^{-3}	-16.409	-5.330	-20.731×10^{-3}
13	0.06925	1.5411	-4.223	-5.288×10^{-3}	0	-2.0047	-4.778×10^{-3}	0	1.8058	6.8138×10^{-3}
21	0.3707	0	1680	0.5609×10^{-3}	66.505	80.512	3.5078×10^{-3}	0.6923	44.255	1.9311×10^{-3}
22	-0.08679	0	1111	0.5529×10^{-3}	0	-34.238	-8.169×10^{-3}	0	-14.993	-5.657×10^{-3}
31	0.06754	0.4762	15238	1.053×10^{-3}	0	27.063	6.457×10^{-3}	0	0.5079	1.916×10^{-3}

Deflections

$$Q_1 \quad \bar{F} = (-20, 49.4, 7.7) \quad \bar{\delta} = (-6.849, 2.151, -5.15) \quad |\delta| = 7.197$$

$$Q_2 \quad \bar{F} = (20, 49.4, 7.7) \quad \bar{\delta} = (5.043, 1.377, -2.38) \quad |\delta| = 5.234$$

Compliances and Their Contributors

Configuration: Vertical Ladder, Position II Material: Aluminum

$$C_{ij} = \frac{10^6}{EI_1} \{K_{u1j} + K_{u1j}\} + \frac{10^6}{EI_2} \{K_{u2j} + K_{u2j}\} + \frac{10^6}{GJ} \{K_{\theta 1j} + K_{\theta 1j}\}$$

$$l_e = 628 \quad e_1 = 9.027 \times 10^6 \quad e_2 = 5263 \times 10^{-3} \times 10^6 \quad e_3 = 2386 \times 10^{-3} \times 10^6$$

$$l_u = 522 \quad e_3 = 10.884 \times 10^6 \quad EI_1 \quad EI_2 \quad GJ$$

ij	C_{ij}	K_{e1}	K_{u1}	$\frac{10^6}{EI_1} \{K_{e1} + K_{u1}\}$	K_{e2}	K_{u2}	$\frac{10^6}{EI_2} \{K_{e2} + K_{u2}\}$	$K_{\theta 1}$	$K_{\theta 2}$	$\frac{10^6}{GJ} \{K_{\theta 1} + K_{\theta 2}\}$
11	2366	82.558	33.666	61.172×10^{-3}	0	4.671	1.115×10^{-3}	4.077	4.5782	174.288
12	16.93	0	-15.197	-7.999×10^{-3}	0	-15.245	-3.637×10^{-3}	-17.42	4.8131	180.955
13	0.05664	1.7801	11.606	12.598×10^{-3}	0	6.897	1.646×10^{-3}	0	-3.864	-14.580
22	2315	0	10.862	5.717×10^{-3}	82.558	62.488	34.608×10^{-3}	0.744	50.589	191.206
23	-0.2164	0	-12.427	-6.541×10^{-3}	0	-23.708	-5.657×10^{-3}	0	-4.062	-15.327
33	0.1466	0.5117	16.909	8.927×10^{-3}	0	18.854	4.498×10^{-3}	0	3.261	1.230

Deflections

$$Q_1 \quad \bar{F} = (-20, 49.7, 5.2) \quad \bar{\delta} = (3.712, 8.007, -1.113) \quad |\delta| = 8.90$$

$$Q_2 \quad \bar{F} = (20, 49.7, 5.2) \quad \bar{\delta} = (-13.176, -14.779, 2.886) \quad |\delta| = 19.82$$

Compliances and Their Contributors

Configuration: Vertical Ladder Position III Material: Aluminum

$$C_{ij} = \frac{10^6}{EI_1} \{ K_{u1ij} + K_{u1ij} \} + \frac{10^6}{EI_2} \{ K_{u2ij} + K_{u2ij} \} + \frac{10^6}{GJ} \{ K_{\theta ij} + K_{\theta ij} \}$$

$$l_e = 565 \quad e_1 = 9.027 \quad \frac{10^6}{EI_1} = 5263 \times 10^{-3} \quad \frac{10^6}{EI_2} = 2386 \times 10^{-3} \quad \frac{10^6}{GJ} = 3.7733 \times 10^{-3}$$

$$l_u = 552 \quad e_3 = 10.884 \quad \frac{10^6}{EI_1} = 5263 \times 10^{-3} \quad \frac{10^6}{EI_2} = 2386 \times 10^{-3} \quad \frac{10^6}{GJ} = 3.7733 \times 10^{-3}$$

i	C_{ij}	K_{e1}	K_{u1}	$\frac{10^6}{EI_1} \{ K_{e1} + K_{u1} \}$	K_{e2}	K_{u2}	$\frac{10^6}{EI_2} \{ K_{e2} + K_{u2} \}$	K_{θ}	$K_{u\theta}$	$\frac{10^6}{GJ} \{ K_{\theta} + K_{u\theta} \}$
11	0.5504	60.121	3.297	33.379×10^{-3}	0	15.863	3.785×10^{-3}	3668	4.3700	17.873×10^{-3}
12	0.9159	0	-6.463	-3.391×10^{-3}	0	9.795	2.337×10^{-3}	-1567	24.708	92.639×10^{-3}
13	-0.05355	14.408	4.101	2.917×10^{-3}	0	6.293	1.502×10^{-3}	0	-2.590	-9.773×10^{-3}
22	55.91	0	26.755	14.082×10^{-3}	60.121	13.684	17.610×10^{-3}	0.669	139.697	527.37×10^{-3}
23	-0.7267	0	-35.125	-18.487×10^{-3}	0	4.497	1.073×10^{-3}	0	-14.645	-55.260×10^{-3}
33	0.3655	0.4604	56.992	30.021×10^{-3}	0	3.101	0.740×10^{-3}	0	1.552	5.792×10^{-3}

Deflections

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$$Q_1 \quad \bar{F} = (-20, 49.9, 2.4) \quad \bar{\delta} = (3.457, 25.893, -3.431) \quad |\delta| = 26.35$$

$$Q_2 \quad \bar{F} = (20, 49.9, 2.4) \quad \bar{\delta} = (-5.658, -29.556, 3.646) \quad |\delta| = 30.313$$

Compliances and Their Contributors

Configuration: Vertical Ladder, Position IV Material: Aluminum

$$C_{ij} = \frac{10^6}{EI_1} \{ K_{11ij} + K_{41ij} \} + \frac{10^6}{EI_2} \{ K_{22ij} + K_{42ij} \} + \frac{10^6}{GJ} \{ K_{33ij} + K_{43ij} \}$$

$$l_1 = 715 \quad e_1 = 9.027 \quad \frac{10^6}{EI_1} = 5263 \times 10^{-3} \quad \frac{10^6}{EI_2} = 2386 \times 10^{-3} \quad \frac{10^6}{GJ} = 3.7733 \times 10^{-2}$$

$$l_4 = 552 \quad e_3 = 10.884 \quad \frac{10^6}{EI_1} = 5263 \times 10^{-3} \quad \frac{10^6}{EI_2} = 2386 \times 10^{-3} \quad \frac{10^6}{GJ} = 3.7733 \times 10^{-2}$$

ij	C_{ij}	K_{e1}	K_{41}	$\frac{10^6}{EI_1} \{ K_{e1} + K_{41} \}$	K_{e2}	K_{42}	$\frac{10^6}{EI_2} \{ K_{e2} + K_{42} \}$	K_{e3}	K_{43}	$\frac{10^6}{GJ} \{ K_{e3} + K_{43} \}$
11	0.7124	121.84	5.202	66.866×10^{-3}	0	12.737	3.039×10^{-3}	4.42	0.921	1.337×10^{-2}
12	-0.2118	0	13.554	7.136×10^{-3}	0	36.433	8.693×10^{-3}	-1.923	-4.684	-3.7002×10^{-2}
13	-0.0417	2.3674	-11.624	-4.904×10^{-3}	0	-3.249	-7.75×10^{-3}	0	4.129	1.262×10^{-2}
22	9.692	0	40.416	21.272×10^{-3}	121.84	104.640	54.035×10^{-3}	0.847	236.801	8.9284×10^{-2}
23	-0.8698	0	-43.493	-22.892×10^{-3}	0	-9.327	-1.302×10^{-3}	0	-20.871	-2.782×10^{-2}
33	0.3250	0.583	60.165	31.657×10^{-3}	0	33.14	1.98×10^{-2}	0	13.29	6.24×10^{-2}

Deflections

$$Q_1 \quad \bar{F} = (-20, 50, 0) \quad \bar{\delta} = (-2.484, 4.8884, -4.261) \quad |\delta| = 4.913$$

$$Q_2 \quad \bar{F} = (20, 50, 0) \quad \bar{\delta} = (3.64, 4.8036, -4.437) \quad |\delta| = 4.824$$

Compliances and Their Contributors

Configuration: Vertical Ladder Position I Material: CRES

$$C_{ij} = \frac{10^6}{EI_1} \{ K_{Lij} + K_{Wij} \} + \frac{10^6}{EI_2} \{ K_{Eij} + K_{Wij} \} + \frac{10^6}{GJ} \{ K_{Eij} + K_{Wij} \}$$

$$L_1 = 584.33 \quad e_1 = 6.352 \quad \frac{10^6}{EI_1} = 51677 \times 10^{-3} \quad \frac{10^6}{EI_2} = 16483 \times 10^{-3} \quad \frac{10^6}{GJ} = 26094 \times 10^{-3}$$

$$L_2 = 552 \quad e_2 = 10.875 \quad \frac{10^6}{EI_1} = 51677 \times 10^{-3} \quad \frac{10^6}{EI_2} = 16483 \times 10^{-3} \quad \frac{10^6}{GJ} = 26094 \times 10^{-3}$$

ij	C_{ij}	K_{E1}	K_{W1}	$\frac{10^6}{EI_1} \{ K_{E1} + K_{W1} \}$	K_{E2}	K_{W2}	$\frac{10^6}{EI_2} \{ K_{E2} + K_{W2} \}$	K_{E3}	K_{W3}	$\frac{10^6}{GJ} \{ K_{E3} + K_{W3} \}$
11	2211	66.505	35.269	52.594×10^{-3}	0	1506	02422×10^{-3}	3794	164.200	168.51×10^{-3}
12	-01309	0	1.500	7752×10^{-3}	0	2.8337	4671×10^{-3}	-1619	-5.3318	-14.335×10^{-3}
13	004533	1.0844	-6707	2138×10^{-3}	0	-2.0027	-3301×10^{-3}	0	1.5049	4.7096×10^{-3}
21	02564	0	1288	0666×10^{-3}	66.505	80.512	24.232×10^{-3}	06511	4428	1.336×10^{-3}
22	-006104	0	-1350	-0698×10^{-3}	0	-34.238	-5.643×10^{-3}	0	-1499	-39.115×10^{-3}
23	004702	0.2358	1870	1088×10^{-3}	0	27.062	4.461×10^{-3}	0	05074	1324×10^{-3}

Deflections

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$$Q_1 \quad \bar{F} = (-20, 494, 77) \quad \bar{\delta} = (-5033, 1481, -357) \quad |\delta| = 5259$$

$$Q_2 \quad \bar{F} = (-20, 491, 77) \quad \bar{\delta} = (3.811, -958, -173) \quad |\delta| = 3933$$

Compliances and Their Contributors

Configuration: Vertical Ladder, Position I Material: Carbon/Epoxy

$$C_{ij} = \frac{10^6}{EI_1} \{ K_{u1j} + K_{u1j} \} + \frac{10^6}{EI_2} \{ K_{e2j} + K_{e2j} \} + \frac{10^6}{GJ} \{ K_{e3j} + K_{e3j} \}$$

$$l_1 = 584.33 \quad e_1 = 6.352 \quad \frac{10^6}{EI_1} = \frac{52533 \times 10^{-3}}{EI_1} = \frac{16774 \times 10^{-3}}{GJ} = \frac{10^6}{GJ} = 2.6531 \times 10^{-3}$$

$$l_u = 552 \quad e_3 = 10.884 \quad \frac{10^6}{EI_1}$$

i	C_{ij}	K_{e1}	K_{u1}	$\frac{10^6}{EI_1} \{ K_{e1} + K_{u1} \}$	K_{e2}	K_{u2}	$\frac{10^6}{EI_2} \{ K_{e2} + K_{u2} \}$	K_{e3}	K_{u3}	$\frac{10^6}{GJ} \{ K_{e3} + K_{u3} \}$
1	2249	66.505	35.268	53.521×10^{-3}	0	15062	0.253×10^{-3}	3794	64.280	171.336×10^{-3}
12	-0.1331	0	1.4999	7882×10^{-3}	0	2.8337	4.753×10^{-3}	-16285	-5.3303	-14.572×10^{-3}
13	0.04672	1.0844	-67068	2176×10^{-3}	0	-2.0027	-3359×10^{-3}	0	1.8057	4.791×10^{-3}
22	0.2609	0	12882	0.6775×10^{-3}	66.505	80.512	24.661×10^{-3}	0.6922	44.256	1.3578×10^{-3}
23	-0.06212	0	-12498	-0.7098×10^{-3}	0	-34.238	-5.743×10^{-3}	0	-14.992	-3.978×10^{-3}
33	0.04735	0.2358	18705	11.077×10^{-3}	0	27.062	4.540×10^{-3}	0	0.5079	1.346×10^{-3}

Deflections

$$Q_1 \quad \bar{F} = (-20, 494, 77) \quad \bar{\delta} = (-5.120, 1.507, -3.63) \quad |\delta| = 5.349$$

$$Q_2 \quad \bar{F} = (20, 494, 77) \quad \bar{\delta} = (3.876, 975, -177) \quad |\delta| = 4.001$$

Compliances and Their Contributors

Configuration: Vertical Ladder, Position IV Material: Carbon/Epoxy

$$C_{ij} = \frac{10^6}{EI_1} \{K_{11ij} + K_{41ij}\} + \frac{10^6}{EI_2} \{K_{22ij} + K_{42ij}\} + \frac{10^6}{GJ} \{K_{33ij} + K_{43ij}\}$$

$$l_1 = 7.15 \quad e_1 = 6.352 \quad \frac{10^6}{EI_1} = 52589 \times 10^{-3} \quad \frac{10^6}{EI_2} = 16774 \times 10^{-3} \quad \frac{10^6}{GJ} = 26531 \times 10^{-6}$$

$$l_4 = 552 \quad e_3 = 10884$$

ij	C_{ij}	K_{e1}	K_{41}	$\frac{10^6}{EI_1} \{K_{e1} + K_{41}\}$	K_{e2}	K_{42}	$\frac{10^6}{EI_2} \{K_{e2} + K_{42}\}$	K_{e3}	K_{43}	$\frac{10^6}{GJ} \{K_{e3} + K_{43}\}$
11	07055	121262	5467	6.940×10^{-3}	0	12737	2.137×10^{-3}	4642	0927	1.478×10^{-3}
12	000450	0	13862	7.290×10^{-3}	0	36666	6.113×10^{-3}	-1983	-4634	-12.953
13	-00093	1221	-12040	-5.473×10^{-4}	0	-3249	-5.45×10^{-3}	0	1120	1.095×10^{-3}
22	6376	0	40110	21.023×10^{-3}	121842	104640	27.990×10^{-3}	3847	236361	628.481
23	-07077	0	-43108	-22.822×10^{-3}	0	-9327	-1.565×10^{-3}	0	-20871	-55.75
33	03676	02835	60338	31.746×10^{-3}	0	2311	13.95×10^{-3}	0	1839	1.370×10^{-3}

Deflections

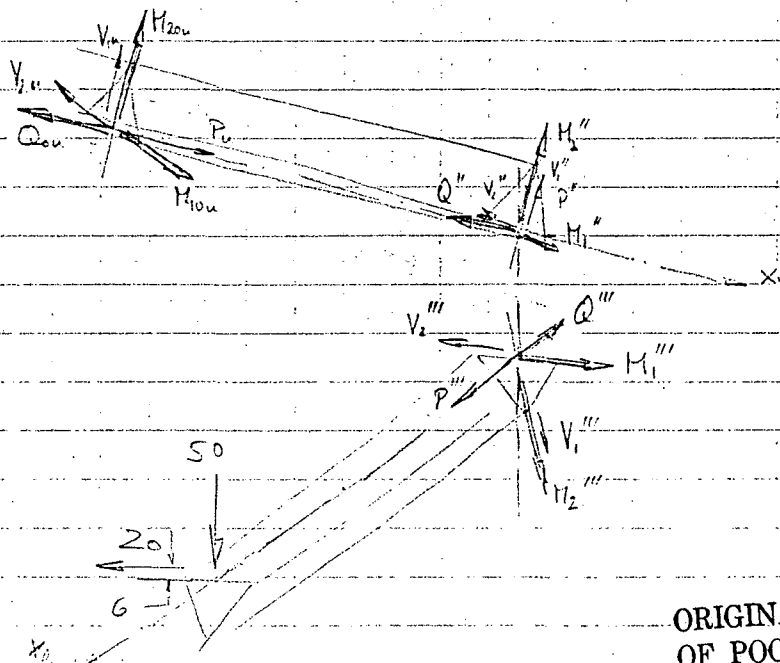
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$$Q_1 \quad \bar{F} = (-20, 50, 0) \quad \bar{\delta} = (-1389, 34371, -3890) \quad |\delta| = 34.62$$

$$Q_2 \quad \bar{F} = (20, 50, 0) \quad \bar{\delta} = (1436, 36380, 1739) \quad |\delta| = 34.46$$

APPENDIX H

HORIZONTAL LADDER CONFIGURATION

Forces in horizontal-ladder barsORIGINAL PAGE IS
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lower arm

$$V_1''' = 49.4$$

$$V_2''' = 20$$

$$P''' = 7.7$$

$$x_c = 0$$

$$H_1''' = 49.4 \times 584.33 = 28,866$$

$$H_2''' = 20 \times 584.33 = 11,687$$

$$Q''' = -120$$

note transformation matrix can be left same as for vertical ladder but force vector is changed to

$\begin{bmatrix} +895 \\ -45.37 \\ 20.26 \\ -10.825 \\ 28.993 \\ 56.83 \end{bmatrix}$	$\begin{bmatrix} -19.95 \\ -46.72 \\ 17.64 \\ 88.11 \\ 28.993 \\ -89.99 \end{bmatrix}$	$\begin{bmatrix} -V_2'' \\ +V_1'' \\ +P'' \\ -H_2'' \\ H_1'' \\ +Q'' \end{bmatrix}$	$= [T]$	$\begin{bmatrix} -V_2''' \\ V_1''' \\ P''' \\ -H_2''' \\ H_1''' \\ Q''' \end{bmatrix}$	$\begin{bmatrix} -20 \\ 49.4 \\ 7.7 \\ -11,687 \\ 28,866 \\ -120 \end{bmatrix}$	$\begin{bmatrix} +20 \\ 49.4 \\ 7.7 \\ 11,687 \\ 28,866 \\ +120 \end{bmatrix}$
---	--	---	---------	--	---	--

then real $V_1'' = -46.72$
 $V_2'' = 19.95$
 $P'' = 17.85$
 $M_1' = 28.595$
 $M_2'' = -8.817$
 $Q'' = -8.999$

at $x_v = l_u - 37.5$ $V_1 = -46.72$

$V_2 = 19.95$

$P = 17.85$

$M_1 = 28.595 - 46.72 \times 37.5 = 26.843$

$M_2 = -8.817 \times 19.95 - 37.5 = -8.063$

$Q = -8.999$

at $x_l = 37.5$ $V_1 = 49.4$

$V_2 = 20$

$P = 7.7$

$M_1 = 28.866 - 49.4 \times 37.5 = 27.014$

$M_2 = 11.687 - 20 \times 37.5 = 10.937$

$Q = -120$

	lower arm		Penl (see page)		upper arm
Q	739.1		2		-119.8
Q_1	163.3				1026.7
Q_2	-894.7				-849.0
Q_3	36.1		4863		-477.3
Q_4	47.7		4863		398.1
Q_5	-35.2		4863		-467.0
Q_6	34.0		10,488		313.0
	panel 1	panel 2		panel 14	panel 15
T_{11}	790.7	764.9	9067	1026.0	684.0
T_{12}	137.5	163.3	9067	684.7	1026.7
T_{13}	-965.7	-823.7	2681	-831.0	-947.0

$M.S = .075$

6-8-78

reverse V_2 to -20at $x_1 = 37.5$ at $x_u = 6 - 37.5$ V_1 49.4 -45.67 V_2 -20 -19.95 P 7.7 20.38 H_1 27,014 27,285 H_2 -10,937 9,575 Q 120 5,683 \bar{r}_1 790.7 960.5 \bar{r}_2 111.7 -36.5 \bar{r}_3 -894.7 -903.7 \bar{r}_4 47.7 237.7 \bar{r}_5 36.1 -315.1 \bar{r}_6 25.2 305.0 \bar{r}_7 -24.0 -208.2 \bar{r}_8 null panel 2 panel 16 panel 18 \bar{r}_9 738.1 512.7 736.6 \bar{r}_{10} 137.5 111.7 127.4 -36.5 \bar{r}_{11} -956.1 -823.5 -847.0 -960.4ORIGINAL PAGE IS
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M.S. = .055

back longeron gets 831 lb compression

Panel must be at least 3×831 lb

$$k_{min} = \frac{\pi^2 E \frac{I}{64} (1.25^4 - 1.0^4)}{L = 37.5^2} > 249.3$$

aluminum $1.0^4 < 453$ not even full root cut

carbon epoxy $1.0 < .9985$ for strength

for stiffness thicker walls may be required

other members (Carbon/Epoxy only)

$$\text{longerons 1, 2} \quad \frac{\pi^3 \cdot 20 \times 10^6 (1.25^4 - 1.0^4)}{64 \times 37.5^2} > 3 \times 1026.7$$

$$1.0 < 1188 \quad (1/32 \text{ wall})$$

$$a\text{-members (4773 lb comp)} \rightarrow 1.0 < 1127$$

d-members less load

note stiffness may require thicker walls

Weight 15 + 20 panels

$$\begin{aligned} & 280.91 \\ & (2 \times 51.204 + 51.205 + 1.5 \times 34.866 + 2 \times 17.5) \cdot 39396 \\ & + 39.5 \times .4882 \\ & + 34.866 \times .2532 \\ & 37.5 \times .0769 \end{aligned}$$

$$\begin{aligned} & 110.67 \\ & 18.31 \\ & 8.13 \\ & 2.6 \\ & \hline & 139.71 \end{aligned}$$

@ .057 lb/in² \rightarrow 7.966 lb/panel
153.3 lower / 119.5 upper

66

for deformations matrix is slightly different

$$\text{because } Q'' - Q_0 l = -V_2''' l \quad H_1''' = V_1''' l \quad H_2''' = V_2''' l$$

$$\begin{bmatrix} -V_{2u} \\ +V_{1u} \\ P_u \\ -H_{2u} \\ H_{1u}' \\ Q_u \end{bmatrix} = \begin{bmatrix} T_{11} & T_{12} & T_{13} \\ T_{21} & T_{22} & T_{23} \\ T_{31} & T_{32} & T_{33} \\ [T_{41} + T_{44} l + T_{46} b] & T_{42} + T_{45} l & T_{43} \\ [T_{51} - T_{54} l + T_{56} b] & T_{52} + T_{55} l & T_{53} \\ [T_{61} + T_{64} l + T_{66} b] & T_{62} + T_{65} l & T_{63} \end{bmatrix} \begin{bmatrix} -V_2''' \\ V_1''' \\ P' \end{bmatrix}$$

different

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or

$$\begin{bmatrix} V_{1u} \\ V_{2u} \\ P_u \\ H_{1u}' \\ V_1' \\ Q_u \end{bmatrix} = \begin{bmatrix} T_{22} & -T_{21} & T_{23} \\ -T_{12} & T_{11} & -T_{13} \\ T_{32} & -T_{31} & T_{33} \\ T_{52} & -T_{51} & T_{53} \\ -T_{62} & T_{61} & -T_{63} \end{bmatrix} \begin{bmatrix} V_1'' \\ V_2' \\ ? \end{bmatrix}$$

new matrix for upper arm terms

$$[T_{\Delta}] = \begin{bmatrix} -85429 & -026228 & -51913 \\ 010525 & -99765 & -067725 \\ 51968 & -0633205 & -85201 \\ \cancel{592608} & -97212 & -62106 \\ \cancel{56035} & & \\ 15580 & & \\ \cancel{14732} & -47839 & -16323 \\ -37613 & & \\ \cancel{-35566} & -35815 & 39410 \end{bmatrix}$$

note - lower arm $Q(x) = -V_2 x - V_2 e_3 = -V_2 (e_3 + x)$

$$\text{then } \frac{\partial U_1}{\partial V_1} = V_1 \frac{1}{EI_1} \frac{l_1^3}{3} + P \frac{e_1 l_1^2}{2EI_1}$$

$$\frac{\partial U_1}{\partial V_2} = \frac{1}{2} \left(\frac{l_1^3}{3EI_2} + \frac{(e_3 + x)^2 l_1}{GJ} \right)$$

$$\frac{\partial U_1}{\partial P} = V_1 \frac{e l_1^2}{2EI_1} + P \frac{e l_1^2}{EI_1}$$

for numerical values assume wall thickness that

produce approximately a 275 lb force

all main members same ID except knee braces ID = 11.
and back scissor (.5 OD / 4 ID)

then length of tubing per panel

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$$2a + 2b + d + 15b = 318 \text{ in}$$

$$\text{total number of panels } 35 \rightarrow \frac{111645 \text{ in}}{318} = 351$$

length of knee braces and	1220	A =	2332	V =
scissor	1313	B =	0700	
in all scissor	1-12	A =	4822	1-6

275 lb \rightarrow allow total volume of 4.835 in^3
for structural knee, 4.447 in^3 or 390 in^3 corr.

$$ID = 1.027$$

note scissor needs thicker wall

$$ID_s = .97 \rightarrow ID_{\text{scissor}} = 1.034 \text{ use } 1.03$$

$$\frac{1}{E_1} = \frac{1}{30,194} - \frac{1}{50,194} \frac{L}{\pi} \left(\frac{1}{2(1.25^2 - 1.03^2)} + \frac{1}{(1.25^2 - 1.03^2)} \right) = 18195 \times 10^{-9}$$

$$\frac{1}{E_2} = \frac{2}{30,194} \frac{1}{20,194} \frac{L}{\pi (1.25^2 - 1.03^2)} = 20380 \times 10^{-9}$$

$$e_1 = 30,194 \frac{1}{1 + 2 \frac{(1.25^2 - 1.03^2)}{(1.25^2 - .97^2)}} = 11,531$$

$$e_3 = 30,194 \frac{(1 - \frac{57,204}{375} + \frac{3}{7} (\frac{34,867}{375})^3)}{(1 + \dots)} = 12,556$$

$$\frac{1}{G_1} = \frac{375}{30,194} - \frac{10^{-5}}{20,194} = 14280 \times 10^{-9}$$

Compliances and Their Contributors

Configuration: Horizontal Ladder Position I Material: Carbon/Epoxy

$$C_{ij} = \frac{10^6}{EI_1} \{K_{u1ij} + K_{w1ij}\} + \frac{10^6}{EI_2} \{K_{u2ij} + K_{w2ij}\} + \frac{10^6}{GJ} \{K_{\theta 1ij} + K_{\theta 2ij}\}$$

$$l_1 = 524.33 \quad e_1 = 11.551 \quad \frac{10^6}{EI_1} = 18195 \times 10^{-3} \quad \frac{10^6}{EI_2} = 20880 \times 10^{-3} \quad \frac{10^6}{GJ} = 14280 \times 10^{-3}$$

$$l_u = 562.5 \quad e_3 = 13.556 \quad EI_1, \quad EI_2, \quad GJ$$

$i-j$	C_{ij}	K_{u1}	K_{w1}	$\frac{10^6}{EI_1} \{K_{u1} + K_{w1}\}$	K_{u2}	K_{w2}	$\frac{10^6}{EI_2} \{K_{u2} + K_{w2}\}$	$K_{\theta 1}$	$K_{\theta 2}$	$\frac{10^6}{GJ} \{K_{\theta 1} + K_{\theta 2}\}$
11	0.2845	66.505	83.054	27.212×10^{-3}	0	19566	04.07×10^{-3}	0	80.184	1.193
12	0.1077	0	-3.2615	-59.34×10^{-3}	0	-1.9071	-39.82×10^{-3}	0	7.9020	11.758
13	-0.06639	1.9721	-37.355	-6.4379×10^{-3}	0	-22625	04.724×10^{-3}	0	-10321	-1.5358
22	137.80	0	18901	034.39×10^{-3}	66.505	36.770	21.564×10^{-3}	22347	77.872	116.206
23	-0.00808	0	2.3878	4.3446×10^{-3}	0	1.2989	27.121×10^{-3}	0	-1.0172	-1.5136
33	0.05688	0.7797	30.718	5.6033×10^{-3}	0	30360	06.444×10^{-3}	0	01323	0.1976

Deflections

$$Q_1 \quad \bar{F} = (49.4, 20, 7.7) \quad \bar{\delta} = (1.570, 3.282, -300) \quad |\delta| = 3.650$$

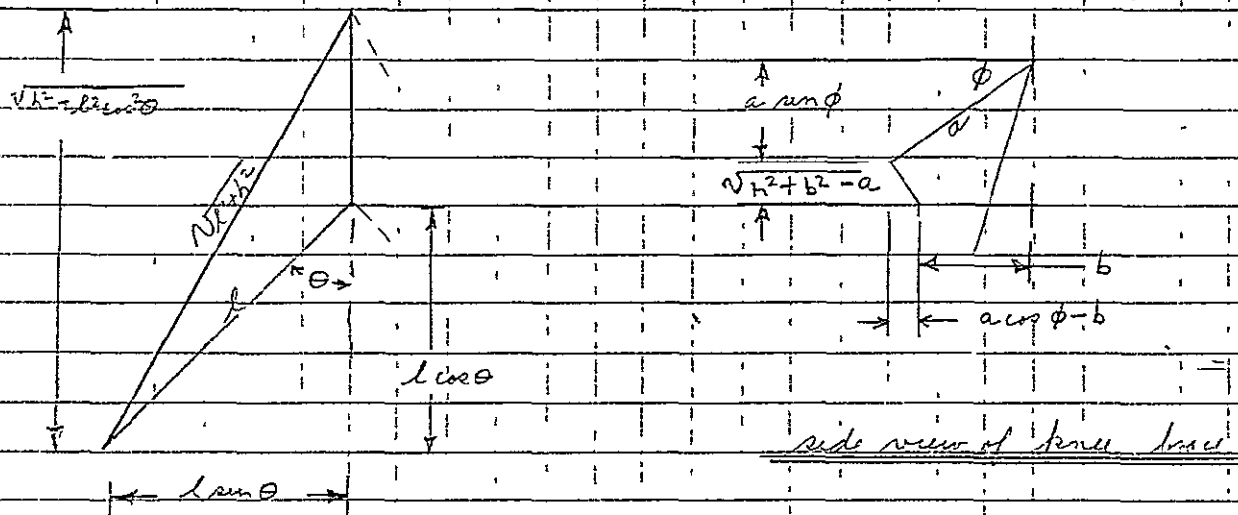
$$Q_2 \quad \bar{F} = (49.1, -20, 7.7) \quad \bar{\delta} = (1.139, -2.230, 328) \quad |\delta| = 2.534$$

APPENDIX I
KNEE BRACE SYNCHRONIZER ANALYSIS

Prepared	Name JC STAMMERMAN	Date 7-11-78	ASTRO RESEARCH CORPORATION	Page / of 11
Checked			TITLE KNEE BRACE SYNCHRONIZER ANALYSIS	Program EVA 1A
Approved				Job No 11792

This analysis is a rewritten copy of Dr. John Hedges's analysis of 5-8-75

Problem - develop a relationship between the knee brace angle, ϕ , and the face panel angle, θ , of the EVATA Truss structure.



b = deployed depth of truss

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top view of knee brace

setting top view equal to side view:

$$\sqrt{h^2 + l^2 \cos^2 \theta} - l \cos \theta = a \sin \phi + \sqrt{h^2 + a^2 \sin^2 \phi + 2ab \cos \phi - 2a \sqrt{h^2 - b^2}}$$

divide by l and solve for $\cos \theta$

$$\cos \theta = \frac{C^2 - K^2}{2CK}$$

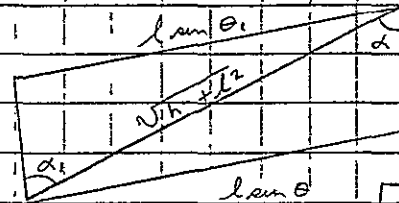
where: $C = h/l$

$$K = \frac{a}{l} \sin \phi + \sqrt{\left(\frac{h}{l}\right)^2 + \left(\frac{a}{l}\right)^2 \sin^2 \phi + 2 \frac{a}{l} \frac{b}{l} \cos \phi - 2 \frac{a}{l} \sqrt{\left(\frac{h}{l}\right)^2 - \left(\frac{b}{l}\right)^2}}$$

Prepared	Name JCS	Date 7-11-78	ASTRO RESEARCH CORPORATION		Page 2 of 1
Checked			TITLE		Program EVATA
Approved					Job No 11792
Preliminary EVATA dimensions					
$l = 33''$					
$b = 18''$					
$h = 22''$					
$a = 23''$					
programming equations C, K into TI 52					
ϕ	θ				
10	17.18				
11	26.64				
10.5	20.88				
12	34.94				
13	41.08				
15	50.14				
20	64.21				
25	72.89				
30	78.79				
35	83.44				
40	86.73				
45	88.94				
46	89.26				
47	89.52				
48	89.74				
49	89.89				
55	89.98				
50.71	90.00				
9.80	5.4				
9.76	2.24				
9.752	1.95				
9.755	1.41				
9.152	0.42				
9.7518	0.23				

Prepared	Name JCS	Date 7-11-78	ASTRO RESEARCH CORPORATION	Page 3 of 11
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Approved			ORIGINAL PAGE IS OF POOR QUALITY	Job No 11792

Effect of inaccuracy



for a given θ , θ is known and

$$\alpha = \sin^{-1} \frac{\sin \theta}{\sqrt{1 + \left(\frac{h}{l}\right)^2}}$$

if the known angle θ is wrong then a difference Δ will occur between α_1 and α

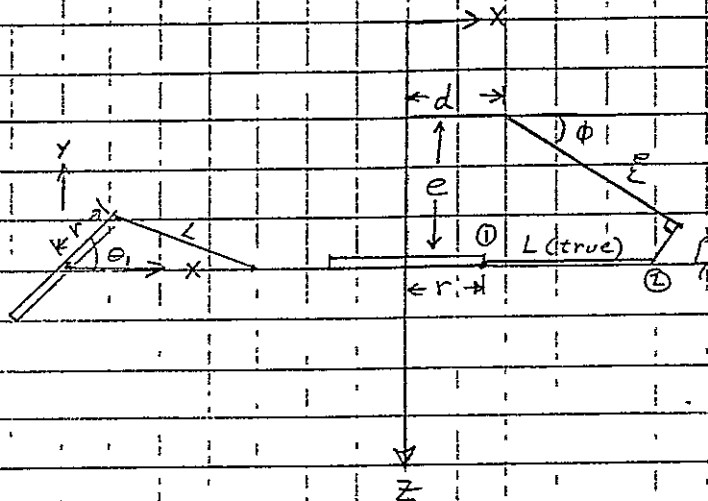
$$\alpha_1 = \alpha + \Delta$$

$$\theta_1 = \sin^{-1} \left(\sqrt{1 + \left(\frac{h}{l}\right)^2} \sin \alpha_1 \right)$$

θ	$\Delta=1$	$\Delta=-1$
5	6.2	3.8
10	11.2	8.8
20	21.2	18.8
30	31.3	28.7
40	41.3	38.7
50	51.5	48.6
60	61.7	58.4
70	72.3	67.9
75	78	72.4
80	85.3	76.6
85	-	79.8
87	-	80.7
90	-	81.2

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Checked			TITLE	Program EUPA
Approved				Job No 11792

Synchronizer Geometry



for point ①

$$x = r \cos \theta_1$$

$$y = r \sin \theta_1$$

$$z = e$$

point ②

$$x = d + \epsilon \cos \phi - \zeta \sin \phi$$

$$y = 0$$

$$z = \epsilon \sin \phi + \zeta \cos \phi$$

$$L^2 = (d + \epsilon \cos \phi - \zeta \sin \phi - r \cos \theta_1)^2 + r^2 \sin^2 \theta_1 + (\epsilon \sin \phi + \zeta \cos \phi - e)^2$$

$$= e^2 + d^2 + \epsilon^2 + \zeta^2 + 2d(\epsilon \cos \phi - \zeta \sin \phi) - 2e(\epsilon \sin \phi + \zeta \cos \phi)$$

$$+ r^2 - 2r \cos \theta_1 (d + \epsilon \cos \phi - \zeta \sin \phi)$$

$$2r(d + \epsilon \cos \phi - \zeta \sin \phi) \cos \theta_1 = r^2 - L^2 + (d + \epsilon \cos \phi - \zeta \sin \phi)^2$$

$$+ (\epsilon \sin \phi + \zeta \cos \phi - e)$$

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Checked			TITLE	Program EVA 7A
Approved				Job No 11792

When $\phi = 50.71^\circ$, $\theta = 90^\circ$ so

$$L^2 = r^2 + (d + \epsilon \cos \phi_s - \zeta \sin \phi_s)^2 + (\epsilon \sin \phi_s + \zeta \cos \phi_s - e)^2$$

so

$$2r \cos \phi_s = (d + \epsilon \cos \phi_s - \zeta \sin \phi_s) +$$

$$+ \frac{(\epsilon \sin \phi_s + \zeta \cos \phi_s - e)^2 - (\epsilon \sin \phi_s + \zeta \cos \phi_s - e)^2}{d + \epsilon \cos \phi_s - \zeta \sin \phi_s}$$

When $\phi = 9.75^\circ$, $\theta = 0$ so

$$2r = (d + \epsilon \cos \phi_s - \zeta \sin \phi_s) + \frac{(\epsilon \sin \phi_s + \zeta \cos \phi_s - e)^2 - (\epsilon \sin \phi_s + \zeta \cos \phi_s - e)^2}{d + \epsilon \cos \phi_s - \zeta \sin \phi_s}$$

$$\text{let } x = \epsilon \cos \phi_s - \zeta \sin \phi_s$$

$$z = \epsilon \sin \phi_s + \zeta \cos \phi_s$$

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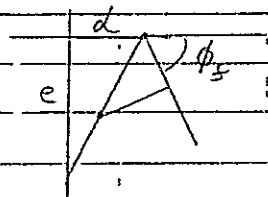
$$\text{then } L^2 - r^2 = (d + x)^2 + (e - z)^2$$

$$r = d - x + \frac{(e - z)^2 - [L^2 - r^2]}{2(d + x)}$$

$$\cos \theta_s = \frac{(d + x)^2 + (e - z)^2 - [L^2 - r^2]}{d + x}$$

$$z - r$$

we have "lookup" at $\phi = \phi_s$ when



$$e = -\frac{z_s}{x_s} d$$

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Checked			TITLE	Program EVATA
Approved				Job No 11792

Partial Rotation

assume that $\theta_1(\phi_1) = 0$

$$\theta_1(\phi_2) = \theta_0 + 90^\circ$$

$$\text{since } Zr \cos \theta_1 = \frac{(d+x)^2 + (e-z)^2 - [L^2 - r^2]}{d+x}$$

$$Zr = \frac{(d+x_1)^2 + (e-z_1)^2 - [L^2 - r^2]}{d+x_1}$$

$$Zr \cos \theta_0 = \frac{(d+x_2)^2 + (e-z_2)^2 - [L^2 - r^2]}{d+x_2}$$

$$L^2 - r^2 = \frac{(d+x_1)[(d+x_2)^2 + (e-z_2)^2] - (d+x_2) \cos \theta_0 [(d+x_1)^2 + (e-z_1)^2]}{d+x_1 - (d+x_2) \cos \theta_0}$$

$$r = \frac{(d+x_1)^2 + (e-z_1)^2 - (d+x_2)^2 - (e-z_2)^2}{2[d+x_1 - (d+x_2) \cos \theta_0]}$$

$$r = \frac{d(x_1 - x_2) + e(z_2 - z_1)}{d+x_1 - (d+x_2) \cos \theta_0}$$

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$$\text{if } \frac{d\theta_1}{d\phi} = 0 \text{ at } \phi = \phi_2$$

$$\frac{d}{d\phi} \left[\frac{(d+x)^2 + (e-z)^2 - [L^2 - r^2]}{d+x} \right]_{\phi = \phi_2}$$

$$\text{if } \frac{dx}{d\phi} = -z, \frac{dz}{d\phi} = x$$

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$$\frac{(d+x_5)^2 + (e-z_5)^2 - [L^2 - r^2]}{d+x_5} = 2 \frac{d z_5 + e x_5}{z_5}$$

substituting,

$$\frac{d z_5 + e x_5}{z_5} = \frac{(d+x_1)^2 + (e-z_1)^2 - (d+x_5)^2 - (e-z_5)^2}{2[d+x_1 - (d+x_5)\cos\theta_0]} \cos\theta_0$$

$$= \frac{d(x_1 - x_5) - e(z_1 - z_5)}{d+x_1 - (d+x_5)\cos\theta_0} \cos\theta_0$$

solving for e,

$$e = \frac{d z_5 [d+x_1 - (d+x_5)\cos\theta_0] - z_5 d(x_1 - x_5) \cos\theta_0}{-x_5 [d+x_1 - (d+x_5)\cos\theta_0] + z_5 (z_5 - z_1) \cos\theta_0}$$

$$e = \frac{d z_5 (d+x_1) (1 - \cos\theta_0)}{x_5 (d+x_1) - [x_5 (d+x_5) - z_5 (z_5 - z_1)] \cos\theta_0}$$

$$= - \frac{d z_5}{x_5} \frac{1 - \cos\theta_0}{1 - \left(\frac{d+x_5}{d+x_1}\right) \cos\theta_0 - \left(\frac{z_5}{x_5}\right) \left(\frac{z_5 - z_1}{d+x_1}\right)}$$

and

$$r = \frac{1 - \frac{d+x_5}{d+x_1} + e \frac{z_5 - z_1}{d+x_1}}{1 - \frac{d+x_5}{d+x_1} \cos\theta_0}$$

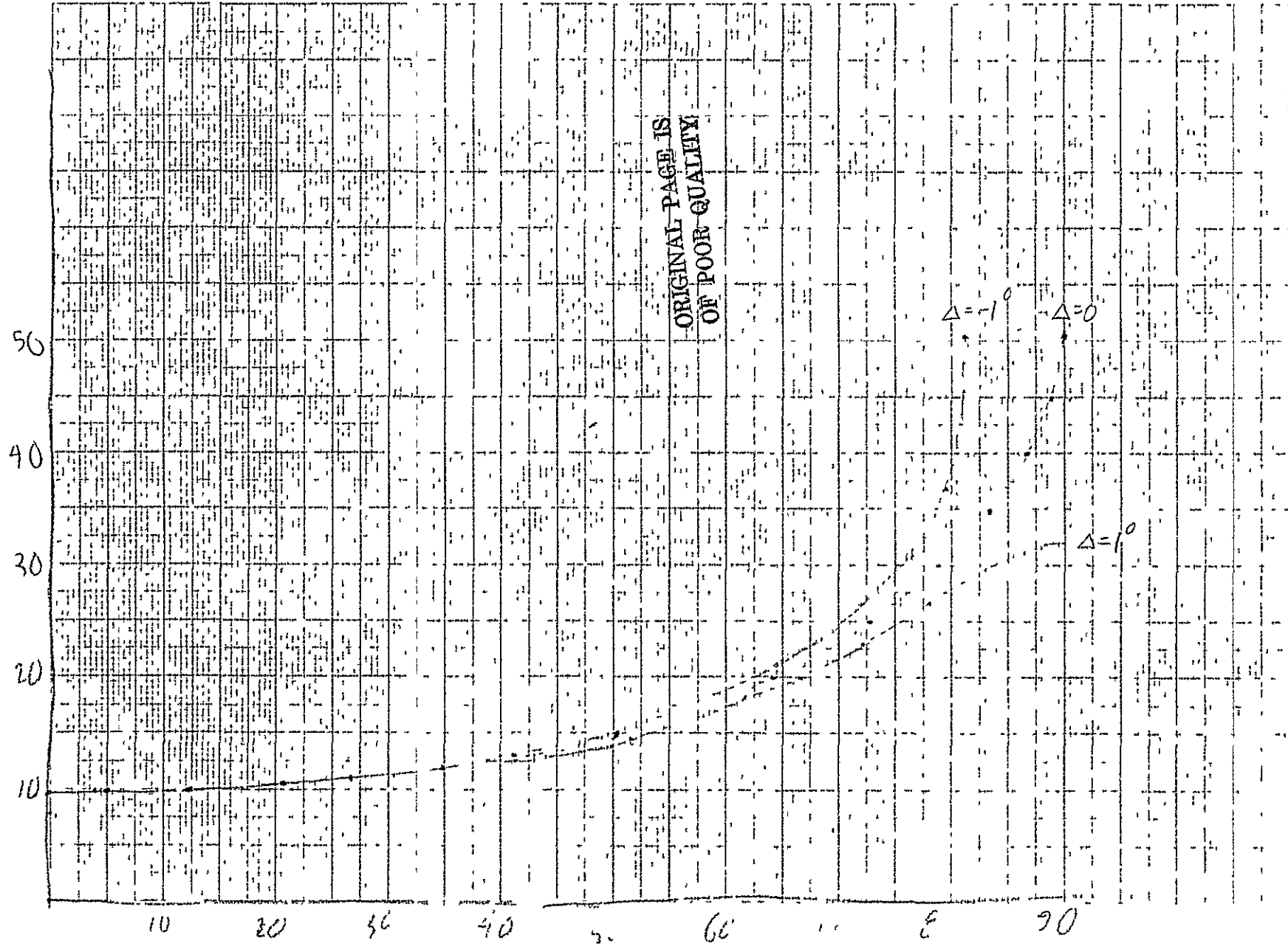
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$$\text{for } d=1, \phi_s = 50.71$$

ϵ	ρ	ϕ_1	θ_0	ϵ	$L^2 - r^2$	r	L
1	0	9.75	7.5	-2.183			
1	1	9.75	6.5	2.637	1.44126	1.11651	1.63947
1	2	9.75	6.5	1.5286			
2	2	9.75	6.5	2.0621	1.31343	1.28842	1.3683
2	2	113	50	1.4410	1.32336	1.1681	1.63946
1	1	113	50	1.90772	-0.19897	1.07486	9.7819

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